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BENCHMARKING SELECTION OF PARAMETER VALUES FOR THE BARCELONA BASIC MODEL

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ABSTRACT

Seven teams took part in a benchmarking exercise on selection of parameter values for the Barcelona Basic Model (BBM) from experimental data on an unsaturated soil. All teams were provided with experimental results from 9 tests performed on a compacted soil in order to determine values for the ten BBM soil constants and an initial value for the hardening parameter. The coordinating team then performed simulations (at stress point level) with the 7 different sets of parameter values, in order to explore the implications of the differences in parameter values and hence to investigate the robustness of existing BBM parameter value selection procedures. The major challenge was found to be selection of values for the constants $\lambda(0)$, r , β , $N(0)$ and p^c and an initial value for the hardening parameter $\bar{p}_0(0)$, with the various teams proposing significantly different values for some of these key parameters. A key lesson emerging from the exercise is the importance of choosing a method for selecting values for the parameters β and p^c which places the main emphasis on attempting to optimise the match to the experimental spacing of normal compression lines at different values of suction.

INTRODUCTION

This paper describes a benchmarking exercise on selection of parameter values for the Barcelona Basic Model (a widely used elasto-plastic constitutive model for the mechanical behaviour of unsaturated soils) from experimental data. This benchmarking exercise was organised within a ‘Marie Curie’ Research Training Network on ‘Mechanics of Unsaturated Soils for Engineering’ (MUSE) (Gallipoli et al., 2006; Toll et al., 2009), which was supported financially by the European Commission. The activities undertaken by the MUSE Network included a variety of benchmarking exercises relating to experimental techniques, constitutive modelling and numerical modelling (see, for example, Tarantino et al., 2011 and D’Onza et al., 2011).

The Barcelona Basic Model (BBM), developed by Alonso et al. (1990) is the earliest and most widely used elasto-plastic constitutive model for unsaturated soils. It has been implemented in a number of finite element codes and has been applied in the numerical analysis of real boundary value problems, including earthworks (e.g. Alonso et al., 2005), field tests (e.g. Costa et al., 2008) and underground disposal of nuclear waste (e.g. Gens et al., 2009). Dissemination and use of the BBM outside the unsaturated soils research community has however been relatively limited, and possible contributory factors in this have been uncertainty in how best to select BBM model parameter values from laboratory test data and concerns on the robustness of such parameter value selection procedures. The benchmarking exercise was designed to investigate these issues.

7 teams took part in the benchmarking exercise: the University of Glasgow, UK (GU); the University of Durham, UK (DU); the Università degli Studi di Trento, Italy (UNITN), the École National des Ponts et Chaussées, France (ENPC); the Università degli Studi di Napoli Federico II, Italy (UNINA), the Universität Innsbruck, Austria (UNINN); and the University of Strathclyde, UK (USTRAT). The first 5 of these were members of the MUSE Network and the last 2 were external participants. The exercise was coordinated from the University of Glasgow (GU).

All 7 teams were provided with the same set of experimental data from a programme of laboratory tests on a single compacted soil. Each team then used the laboratory test data to select BBM parameter values for the soil, with complete freedom on the methodology they employed for selection of parameter values. Each team returned to GU their selected BBM parameter values, together with details of the procedure they had employed in selection of parameter values. The team at GU then performed simulations with the 7 different sets of parameter values. These simulations were performed at stress point level (rather than for boundary value problems), and they included simulations of the full set of laboratory tests that the teams had used in the selection of parameter values, but also several fictitious stress paths and various other features of model performance. Comparisons between the simulation results with the 7 different parameter value sets were used to explore the implications of the differences in parameter values and hence to investigate the robustness of BBM parameter value selection procedures.

BARCELONA BASIC MODEL

The Barcelona Basic Model (BBM), developed by Alonso et al. (1990), uses mean net stress \bar{p} , deviator stress q and matric suction s as stress state variables, where \bar{p} is the excess of mean total stress over pore air pressure and s is the difference between pore air pressure and pore water pressure. The model implicitly assumes that saturated conditions are achieved whenever s is zero, and only when s is zero, and at this limit the BBM converges with the Modified Cam Clay model for saturated soils (Roscoe and Burland, 1968). The BBM is intended for use with unsaturated fine-grained soils, but excluding those containing highly expansive clay minerals.

In the formulation of BBM, elastic volumetric strain increments are given by:

$$d\varepsilon_v^e = \kappa \frac{d\bar{p}}{\bar{p}} + \kappa_s \frac{ds}{v(s + p_{at})} \quad (1)$$

where v is the specific volume, p_{at} is atmospheric pressure and κ and κ_s are two elastic soil constants. The term involving κ represents elastic volume changes caused by variation of \bar{p} , giving elastic unloading/reloading lines of gradient κ in the $v:\ln \bar{p}$ plot, whereas the term involving κ_s represents elastic volume changes caused by variation of s (swelling on wetting and shrinkage on drying), giving shrink/swell lines of gradient κ_s in the $v:\ln(s + p_{at})$ plot. Atmospheric pressure p_{at} is (rather arbitrarily) included within Equation (1) in order to avoid infinite elastic volumetric strains as suction tends to zero.

Elastic shear strain increments are given by:

$$d\epsilon_s^e = \frac{dq}{3G} \quad (2)$$

where G is the elastic shear modulus (a soil constant).

Isotropic normal compression lines for different values of suction are all assumed to be straight lines in the $v:\ln \bar{p}$ plot, defined by:

$$v = N(s) - \lambda(s) \ln \left(\frac{\bar{p}}{p^c} \right) \quad (3)$$

where p^c is a reference pressure (a soil constant) and the intercept $N(s)$ (defined at the reference pressure p^c) and gradient $\lambda(s)$ are both functions of suction s .

The variation of $N(s)$ with suction is assumed as:

$$N(s) = N(0) - \kappa_s \ln \left(\frac{s + p_{at}}{p_{at}} \right) \quad (4)$$

where $N(0)$ (a soil constant) is the value of $N(s)$ at zero suction (the intercept of the saturated normal compression line). The assumption that there exists a single value of

\bar{p} (the reference pressure p^c) at which the spacings between the saturated normal compression line and the normal compression lines for all non-zero values of s are given by Equation (4), is a major assumption within the BBM, which was made by Alonso et al. (1990) in order to produce subsequently a relatively simple expression for the LC yield curve (see below). This assumption within the model has significant implications for both the positions of the normal compression lines for different values of suction and the development of the shape of the LC yield curve as it expands (see below).

The variation of $\lambda(s)$ with suction is assumed as:

$$\lambda(s) = \lambda(0)[r + (1-r)\exp(-\beta s)] \quad (5)$$

where $\lambda(0)$ (a soil constant) is the value of $\lambda(s)$ at zero suction (the gradient of the saturated normal compression line) and r and β are two further soil constants. Inspection of Equation (5) shows that $\lambda(s)$ varies monotonically with increasing suction, from a value $\lambda(0)$ at zero suction to a limiting value $r\lambda(0)$ as suction tends to infinity, with the soil constant β controlling the rate of exponential approach to this limiting value. If the value of r is less than 1 then $\lambda(s)$ decreases with increasing suction (collapse potential increasing with increasing \bar{p}), whereas if the value of r is greater than 1 then $\lambda(s)$ increases with increasing suction (collapse potential decreasing with increasing \bar{p}). In the former case, the value of the reference pressure p^c will need to be very low (much lower than the range of \bar{p} over which the model is to be applied), whereas in the latter case, the value of p^c will need to be very high (much higher than the range of \bar{p} over which the model is to be applied) (see Wheeler et al., 2002).

For isotropic stress states, the BBM includes a Loading-Collapse (LC) yield curve, defined in the $s: \bar{p}$ plane, which corresponds to the onset of plastic volumetric strain during either isotropic loading (increase of \bar{p}) or wetting (reduction of s). Stress states on the LC yield curve also correspond to points on the isotropic normal

compression lines defined by Equation (3), and hence combination of Equations (1), (3) and (4), leads to the following expression for the shape of the LC yield curve in the BBM:

$$\left(\frac{\bar{p}_0}{p^c} \right) = \left(\frac{\bar{p}_0(0)}{p^c} \right)^{\frac{\lambda(0)-\kappa}{\lambda(s)-\kappa}} \quad (6)$$

where \bar{p}_0 is the yield value of \bar{p} at a suction s and $\bar{p}_0(0)$ is the corresponding value of \bar{p}_0 at zero suction. Equation (6) defines the developing shape of the LC yield curve as it expands during plastic straining (as the value of the hardening parameter $\bar{p}_0(0)$ increases). The relatively simple form of Equation (6) is a consequence of the assumption within the BBM that there exists a single reference pressure p^c at which the spacings of all the normal compression lines for different values of suction are given by Equation (4). Inspection of Equation (6) indicates that a consequence of this assumption is that the LC yield curve is a vertical straight line in the $s: \bar{p}$ plane when $\bar{p}_0(0) = p^c$, and the developing shape of the LC yield curve as it expands can be traced back to this assumption.

The BBM also includes a second yield curve for isotropic stress states, the Suction-Increase (SI) yield curve, which predicts the onset of plastic volumetric strains if the suction is increased beyond the maximum value previously applied. The laboratory test data used for the benchmarking exercise did not however include any stress paths in which the suction was increased beyond the initial value produced by sample compaction, and hence the SI yield curve was not included in the benchmarking exercise.

To incorporate the role of deviator stress q , the LC yield curve is developed to form a LC yield surface in $q: \bar{p}: s$ space. Constant suction cross-sections of this LC yield surface are assumed to be elliptical in the $q: \bar{p}$ plane, with an intercept $\bar{p}(0)$ on the positive \bar{p} axis (on the LC yield curve), an intercept $-ks$ on the negative \bar{p} axis and an aspect ratio M :

$$q^2 = M^2(\bar{p} + ks)(\bar{p}_0 - \bar{p}) \quad (7)$$

where M and k are two final soil constants. At zero suction, Equation (7) converges to the Modified Cam Clay yield curve equation for saturated soil. The full shape of the LC yield surface in $q: \bar{p}:s$ space is defined by the combination of Equations (6) and (7).

The hardening law for yielding on the LC yield surface relates plastic volumetric strain to the expansion of the yield surface (represented by increase of the saturated isotropic yield stress $\bar{p}_0(0)$):

$$d\varepsilon_v^p = (\lambda(0) - \kappa) \frac{d\bar{p}_0(0)}{v\bar{p}_0} \quad (8)$$

The flow rule for yielding on the LC yield surface gives the ratio of plastic shear strain increment to plastic volumetric strain increment as:

$$\frac{d\varepsilon_s^p}{d\varepsilon_v^p} = \frac{2q\alpha}{M^2(2\bar{p} + ks - p(0))} \quad (9)$$

where α is a constant. $\alpha = 1$ would correspond to an associated flow rule, but Alonso et al. (1990) suggest a value for α selected in order to give zero lateral strain during elasto-plastic loading of a saturated sample at a stress ratio approximating to Jaky's simplified formula for the normally consolidated value of K_0 . This value of α can be expressed in terms of $\lambda(0)$, κ and M (see Alonso et al., 1990), and this was the expression for α used within the benchmarking exercise.

As a consequence of the flow rule and the hardening law (Equations (9) and (8)), the BBM predicts the occurrence of critical states for stress states which correspond to the apex of the elliptical constant suction cross-sections of the LC yield surface. As a consequence, critical state lines for different values of suction are defined in the $q: \bar{p}$ plane by:

$$q = M\bar{p} + Mks \quad (10)$$

The BBM therefore assumes linear increases of critical state strength with both net stress and suction, equivalent to the unsaturated shear strength expression proposed by Fredlund et al. (1978) (with $c' = 0$).

The form of the critical state lines for different values of suction in the $v: \ln \bar{p}$ plane predicted by the BBM is given by:

$$v = N(s) - (\lambda(s) - \kappa) \ln \left(2 + \frac{ks}{\bar{p}} \right) - \lambda(s) \ln \left(\frac{\bar{p}}{p^c} \right) \quad (11)$$

Inspection of Equation (11) indicates that each constant suction critical state line is curved in the $v: \ln \bar{p}$ plane (except for the saturated critical state line corresponding to $s = 0$). Comparison with Equation (3) shows that, at high values of \bar{p} , each constant suction critical state line asymptotically approaches a straight line that is parallel to the corresponding constant suction normal compression line.

If the SI yield surface is excluded, the BBM involves 10 soil constants: κ , κ_s , G , p^c , $N(0)$, $\lambda(0)$, r , β , M and k . In addition, specification of the initial state of the soil requires not just the initial stress state (initial values of \bar{p} , q and s) but also the initial value of the hardening parameter $\bar{p}_0(0)$, defining the initial position of the LC yield surface.

EXPERIMENTAL DATA

The laboratory test data used for the benchmarking exercise were from tests performed at Universitat Politècnica de Catalunya (UPC), reported in the PhD thesis of Barrera Bucio (2002). 9 tests from the PhD thesis were used for the benchmarking exercise, and all participating teams were requested not to read the thesis or related

publications, so that the only information that they used was that provided directly through the benchmarking exercise.

Soil properties

The experimental tests were performed on compacted samples of a natural soil that was obtained during excavation works for the construction of the Rector Gabriel Ferrate Library on the North Campus of UPC in Barcelona, Spain. The soil consisted of 44.5% silt fraction, 39.4% sand fraction and 16.1% clay fraction (mainly illitic). The particle size distribution is given in Figure 1(a). The soil had a plastic limit of 16% and a liquid limit of 32%, and the specific gravity G_s of the soil particles was 2.71.

Sample preparation

Samples were prepared by static compaction at a water content of $11\% \pm 0.2\%$ by applying an isotropic confining pressure of 600 kPa. Figure 1(b) shows the compaction curve produced by this method of compaction (isotropic static compaction under an all-round stress of 600 kPa), with the sample compaction condition indicated by the solid circular data point. This shows that samples were compacted approximately 3% dry of the optimum corresponding to this particular compaction method.

Total suction after compaction was measured by psychrometer as 800 kPa. The majority of samples were subsequently subjected to an initial equalisation stage under low mean net stress and a matric suction s of 800 kPa. Negligible volume change was observed during such stages, indicating that the matric suction after compaction was approximately 800 kPa, and hence that osmotic suction was negligible in these samples. Contours of total suction measured post-compaction are shown in the compaction plot of Figure 1(b).

The initial conditions (immediately following compaction) of each of the 9 samples are presented in Table 1 in terms of initial diameter D_0 , initial height H_0 , initial void ratio e_0 and initial degree of saturation S_{r0} .

Experimental tests

The experimental dataset provided to the participating teams consisted of the results of 9 tests, including two isotropic tests (Figure 2), six triaxial tests (Figure 3) and one oedometer test (Figure 4). For testing of unsaturated samples, control of matric suction was by the axis translation technique.

Test SAT-1 (Figure 2(a)) was an isotropic test performed on a saturated sample, involving initial saturation by flushing through (AB in Figure 2(a)) and then isotropic loading (BC) to a mean effective stress of 1300 kPa, followed by isotropic unloading (CD).

Test TISO-1 (Figure 2(b)) was a suction-controlled isotropic test performed on an unsaturated sample. This involving isotropic loading (AB) at a constant suction of 800 kPa to a mean net stress of 600 kPa, wetting (BC) and subsequent drying (CD) at constant mean net stress to a suction of 10 kPa and then back to a suction of 150 kPa, isotropic loading (DE) and unloading (EF) at constant suction to a mean net stress of 1400 kPa and then back to 600 kPa, wetting (FG) to a suction of 20 kPa, isotropic loading (GH) to a mean net stress of 2000 kPa and then finally isotropic unloading (HI). For both isotropic tests (SAT-1 and TISO-1), changes of mean effective stress, mean net stress or suction were applied as a series of discrete step changes, each followed by an equalisation period, rather than as a continuous ramped process (see later).

5 of the 6 suction-controlled triaxial tests (Figure 3) involved shearing to failure at a constant suction of 800 kPa, whereas the final triaxial test involved shearing to failure at a suction of 20 kPa.

The stress paths followed in triaxial tests IS-OC-03, IS-NC-06 and IS-NC-12 (Figure 3(a),(b) and (c)) involved “isotropic” loading (AB) at a constant suction of 800 kPa (to a mean net stress of 300, 600 or 1200 kPa respectively) followed by shearing to failure (BCDE) at constant suction and constant radial net stress, with the inclusion of an unload-reload cycle during shearing. A small nominal deviator stress of 10 kPa was applied during “isotropic” stages in all triaxial tests, in order to maintain contact between the loading ram and the sample.

Triaxial tests IS-OC-06 and IWS-OC-01 (Figure 3(d) and (e)) also involved shearing to failure at a constant suction of 800 kPa and a constant radial net stress of 600 kPa (including one or two unload-reload cycles during shearing). In the former, however, shearing was preceded by “isotropic” loading (AB) to a mean net stress of 1600 kPa and then “isotropic” unloading (BC), whereas in the latter, shearing was preceded by a wetting-drying cycle (BCD) down to a suction of 10 kPa. The final triaxial test IWS-NC-02 (Figure 3(f)) involved shearing to failure at a constant suction of 20 kPa and a constant radial net stress of 600 kPa, following “isotropic” loading (AB) at a suction of 800 kPa and then wetting (BC) to a suction of 20 kPa.

During “isotropic” loading, unloading, wetting or drying stages of all triaxial tests, changes of mean net stress or suction were applied as a series of discrete step changes, each followed by an equalisation period. In contrast, shearing stages (including unloading-reloading) were performed at a constant axial displacement rate of 1.0 $\mu\text{m}/\text{min}$. Participating teams were told to assume that all stages were performed sufficiently slowly to give essentially uniform conditions throughout the sample.

The single suction-controlled oedometer test EDO-1 (Figure 4) involved loading (AB) at a constant suction of 800 kPa to a vertical net stress $\bar{\sigma}_v$ of 600 kPa, followed by wetting (BC) to a suction of 10 kPa, drying (CD) to a suction of 300 kPa, loading (DE) and unloading (EF) to vertical net stresses of 1600 kPa and 600 kPa respectively, wetting (FG) to a suction of 50 kPa, loading (GH) to a vertical net stress of 2400 kPa and then final unloading (HI). Again each stage of the oedometer test was applied as a series of discrete step changes of vertical net stress or suction, each followed by an equalisation period.

BENCHMARKING METHODOLOGY

Each team participating in the benchmarking exercise was provided with the same information, consisting of a Word file describing soil properties, sample preparation and experimental procedures and Excel files containing the experimental data for the 9 tests. The Excel files contained details of the initial state of each sample immediately following compaction (see Table 1) and the subsequent stress path and stress-strain response for all stages of each test. For isotropic tests, data were provided in terms of mean net stress \bar{p} , suction s and void ratio e , whereas for triaxial tests, data were provided in terms of mean net stress \bar{p} , deviator stress q , suction s , void ratio e and axial strain ε_1 . For the single oedometer test, data were provided in terms of vertical net stress $\bar{\sigma}_v$, suction s and void ratio e .

Each of the 7 participating teams was required to determine, from the experimental data, values for the 10 BBM soil constants (κ , κ_s , G , p^c , $N(0)$, $\lambda(0)$, r , β , M and k) and an initial value for the hardening parameter $\bar{p}_0(0)$. Teams had complete freedom on the methodology they employed in the selection of model parameter values. In practice, 6 of the 7 teams attempted to isolate specific features of behaviour in order to determine the values of different individual model constants, but then generally had to employ some degree of iteration or compromise. These iterations or compromises were necessary because the test data could not, of course, be perfectly matched by the BBM and some of the BBM constants affect more than one aspect of behaviour and also some aspects of behaviour are affected by more than one constant. Different teams also chose to place greater or lesser emphasis on particular aspects of behaviour or on particular individual tests.

The overall approach employed by the team from UNINN was very different to the methodology of the other 6 teams. The team from UNINN performed a formal optimization process using inverse analysis. This involved simultaneous optimization of the values of most of the 10 soil constants and the initial value of the hardening parameter, by attempting to minimize suitable objective functions describing the

differences between model simulations and experimental results. Exceptions were G , M and k , which were determined by the UNINN team in a more conventional fashion.

Each of the 7 teams submitted a return form with their selected values for the 10 BBM soil constants and the initial value of the hardening parameter, together with short descriptions of the procedures that had been employed in estimating these values. The coordinating team from GU compared the 7 parameter value sets, analysed the reasons behind significant differences in proposed parameter values and investigated the implications of these differences. This included performing simulations of all 9 experimental tests with the 7 different sets of parameter values, as well as simulating various fictitious stress paths and investigating other aspects of predicted behaviour.

RESULTS: PARAMETER VALUES

BBM parameter values determined by each of the 7 participating teams are listed in Table 2. The BBM is unable to match perfectly the experimental data used in the benchmarking exercise, and therefore there is no single “correct” answer for the set of parameter values. A particular combination of parameter values may produce a good match to one aspect of experimental behaviour, whereas another combination results in better matching to another aspect of behaviour. The differences in parameter values proposed by the 7 teams may therefore partly reflect different emphasis given to various aspects of the experimental results by the different teams. It is also possible that different combinations of parameter values can give very similar predictions for some stress paths and yet widely different predictions when applied to other stress paths. These issues are considered later in the paper.

The parameters listed in Table 2 can be divided into five groups: BBM constants describing elastic behaviour (κ , κ_s and G); BBM constants giving the variation of $\lambda(s)$ with suction ($\lambda(0)$, r and β); other BBM constants involved in describing yielding and plastic behaviour under isotropic stress states (p^c and $N(0)$); BBM

constants related to soil strength (M and k); and the initial value of the hardening parameter $\bar{p}_0(0)$. Each of these groups is considered in turn.

Elastic parameters κ , κ_s and G

The elastic parameters κ , κ_s and G are generally of relatively minor importance, because elastic strains are typically significantly smaller than plastic strains. Indirect effects of these parameters in the BBM are also normally relatively minor. For example, the value of κ affects the shape of the LC yield curve (through Equation (6)) and the value of κ_s affects the positions of the normal compression lines for different values of suction (through Equation (4)), and hence the values of these two elastic parameters have some influence on the predicted occurrence and magnitude respectively of collapse compression on wetting, but both of these effects are relatively small.

Inspection of Table 2 shows that the values of κ determined by the 7 teams varied from 0.007 to 0.012 . The values can be divided into three groups, with ENPC, UNINA and USTRAT suggesting values close to 0.007, UNITN, GU and UNINN suggesting values close to 0.010 and DU suggesting a value of 0.012. Inspection of the procedures used by the different teams indicates that these groupings were not related to differences in the general methodology employed or in the choices of which parts of the experimental data were used by the teams to determine the value of κ . All teams, with the exception of UNINN (who determined the majority of parameter values in a single global optimisation exercise), used unloading (and sometimes pre-yield loading) data from isotropic tests (and sometimes “isotropic” stages of triaxial tests) to determine a value for κ . It appears that the variation in the values of κ determined by the different teams can be mainly attributed simply to differences in the ways the teams fitted idealised straight lines to the relevant experimental data in a $v:\ln \bar{p}$ plot.

Table 2 shows that all teams suggested relatively low values for the elastic parameter κ_s , consistent with only small magnitudes of elastic swelling or shrinkage induced by suction changes over the experimental range of zero to 800 kPa. However, the values proposed for κ_s by the different teams varied by almost an order of magnitude, from 0.0005 to 0.0045. The experimental data used by teams (with the exception of UNINN) in this determination were from wetting or drying stages considered to be inside the LC yield curve. This potentially covered drying stage CD and wetting stage FG from Test TISO-1 (see Figure 2(b)) and drying stage CD from Test IWS-OC-01 (see Figure 3(e)). The results from TISO-1 covered a much smaller range of suction than those from IWS-OC-01, but they were better defined by a number of intermediate points (whereas there were only two data points, at the start and end of drying, for stage CD of Test IWS-OC-01). As a consequence, different teams made different choices of how much weight to give to the results from the two tests in the determination of a value for κ_s . Inspection showed that there was significant correlation between the emphasis given to the different experimental tests and the value of κ_s determined, with those teams relying exclusively on the results from TISO-1 generally suggesting lower values for κ_s than those who also made use of the results from IWS –OC-01.

Inspection of Table 2 shows that the values of shear modulus G determined by the 7 teams varied from 80 MPa to 200 MPa (but with 5 of the 7 values clustered within a range from 120 MPa to 167 MPa). All teams determined the value of G from the unload-reload stages of the triaxial tests. Differences in the proposed value of G were attributable simply to the details of how the experimental unload-reload stress-strain curves were interpreted e.g. the starting and finishing points used when determining the best-fit straight line to the data, whether unload and reload curves were fitted separately or a single line was fitted to an entire unload-reload loop, and whether stress or strain was used as the dependent variable in a least-squares fitting process.

Plastic compressibility parameters $\lambda(0)$, r and β

The three BBM constants $\lambda(0)$, r and β control the variation of plastic compressibility $\lambda(s)$ with suction, through Equation 5, i.e. they control the gradients of the normal compression lines at different values of suction (Equation 3). However, by determining the gradients of the lines, they also control the spacing between the normal compression lines for different values of suction at all values of mean net stress other than the reference pressure p^c (see Equation 3) i.e. they (together with p^c) control the spacing between the normal compression lines over the range of \bar{p} for which the model will be applied. This means that the three parameters will have an important influence on the predicted magnitude of potential wetting-induced collapse compression and how this varies with \bar{p} . The three parameters also control (together with p^c and, to a lesser degree, κ) the shape of the LC yield curve and how this develops as it expands (see Equation 6) and hence whether collapse compression will occur during a given wetting path.

Most teams (UNINN was the exception) determined values for $\lambda(0)$, β and r predominantly by considering the gradients $\lambda(s)$ of normal compression lines at different values of suction. Several of these teams, however, also took some account of one or more other aspect of behaviour (e.g. the initial shape of the LC yield curve or the spacing between the different normal compression lines).

Experimental results showing normal compression lines during isotropic (or nearly isotropic) loading were available at four different values of suction: $s = 0$ (SAT-1), $s = 20$ kPa (TISO-1), $s = 150$ kPa (TISO-1) and $s = 800$ kPa (IS-NC-12 and IS-OC-06). In addition, experimental results from the oedometer test (EDO-1) gave some information on the normal compression lines produced by one-dimensional loading (at $s = 50$ kPa and $s = 300$ kPa), but this information was not used by most teams. The values of $\lambda(s)$ determined from the experimental data for isotropic loading at the four different values of suction varied slightly between the different teams (simply as a consequence of differences in the way that idealised straight lines were fitted to the experimental data). However, far more important was the fact that the resulting experimental values of $\lambda(s)$ at the four different values of suction did not show a

monotonic variation with s , and hence could not be well-fitted by Equation 5. Each team used a different procedure in attempting to fit Equation 5 to their four experimental values of $\lambda(s)$, including giving different emphases to the four experimental values, and this was the most important factor behind the different values of $\lambda(0)$, β and r determined by the various teams.

Values of $\lambda(0)$, β and r determined by the different teams are given in Table 2 and the corresponding variations of $\lambda(s)$ with suction predicted by the teams are shown in Figure 5.

Inspection of Figure 5 shows that values of $\lambda(s)$ predicted by UNINN at suctions above about 50kPa are substantially higher than those predicted by all other teams, and comparison with the experimental data shows that such high values of $\lambda(s)$ are unrealistic. This indicates the likelihood that the formal optimization process employed by UNINN (involving simultaneous optimisation of multiple parameters) was not successful in identifying a global minimum for the objective function, but instead converged on an inappropriate local minimum. This shows the potential risks of such formal optimisation procedures and emphasises that they should be used only with great caution.

Inspection of Table 2 and Figure 5 shows that the values of $\lambda(0)$ determined by the different teams varied from 0.072 to 0.097. DU, ENPC and UNINA proposed values between 0.072 and 0.074, based exclusively on the gradient measured in the saturated isotropic test SAT-1. GU and USTRAT proposed slightly higher values (0.078 and 0.080), as a consequence of using additional information in the determination of $\lambda(0)$. GU determined values for $\lambda(0)$ and r together, by best-fitting Equation 5 to all experimental values of $\lambda(s)$ (having previously determined a value for β by another method, as described below). USTRAT used results from other low suction test stages (TISO-1 at $s = 20$ kPa and EDO-1 at $s = 50$ kPa) in addition to the saturated test SAT-1 in the determination of a value for $\lambda(0)$, rather than relying exclusively on a single test result. UNITN suggested a significantly higher value (0.097) for $\lambda(0)$ than all other teams, because they ignored the experimental result

from SAT-1, which they considered to be inconsistent with all other results and hence unreliable. UNITN based their value for $\lambda(0)$ on the low suction result from TISO-1 (at $s = 20\text{kPa}$).

Inspection of Table 2 shows that all teams except UNINN proposed a value for r close to 1 and hence simulated relatively little variation of $\lambda(s)$ over the full range of suction (see Figure 5). In contrast, the value proposed by UNINN ($r = 1.814$) results in much larger variation of $\lambda(s)$, including unrealistically large values of $\lambda(s)$ at suctions above about 50kPa, as discussed previously. Of the other teams, GU proposed a value for r slightly greater than 1 ($r = 1.0567$), whereas the remaining teams proposed values slightly less than 1 ($r = 0.8 - 0.875$). The fact that GU proposed a value for r greater than 1 whereas other teams proposed values less than 1 reflects the fact that the full set of experimental values of $\lambda(s)$ did not vary monotonically with suction and could not therefore be well-matched by Equation 5. As a consequence, the value proposed for r depended on the relative weight given to the various experimental values of $\lambda(s)$ and the precise procedure used in fitting Equation 5 to the experimental results.

Values for β suggested by the various teams varied by almost two orders of magnitude, from 0.0017kPa^{-1} to 0.125kPa^{-1} (see Table 2). A low value for β (e.g. ENPC) indicates that $\lambda(s)$ continues to vary over a very wide range of suction, whereas a high value for β (e.g. DU) indicates that variation of $\lambda(s)$ is limited to only the low suction range (see Figure 5). Again, this variation in the values of β proposed by the various teams was generally attributable to differences in the relative weightings given to the experimental values of $\lambda(s)$ and to differences in the procedures used in fitting Equation 5 to the experimental values of $\lambda(s)$. In addition, however, some teams (e.g. ENPC and GU) also took account of some other aspect of experimentally observed behaviour (such as the initial shape of the LC yield curve or the spacings of the normal compression lines at different values of suction) in determining a value for β . In fact, GU did not consider experimental values of $\lambda(s)$ at all in determining a value for β , and their procedure was based entirely on

attempting to fit the relative spacings between the normal compression lines at different values of suction, because they had identified that this important aspect of behaviour is almost solely dependent on the value of β (see below). The GU procedure for selecting the value of β from the relative spacings of the normal compression lines at different values of suction is set out in Gallipoli, D'Onza and Wheeler (2010).

Parameters p^c and $N(0)$

With the variation of $\lambda(s)$ with suction defined by the values of $\lambda(0)$, r and β and with the value of the elastic parameter κ_s already determined, the parameters p^c and $N(0)$ complete the definition of the normal compression lines for different values of suction (see Equations 3 and 4), by fixing the position of each line. In addition, the value of p^c (along with the parameters determining $\lambda(s)$ and the elastic parameter κ) defines the shape of the LC yield curve and how this develops as it expands (see Equation 6).

With the exception of UNINN, teams determined a value for p^c either from the experimental evidence on the initial shape of the LC yield curve (DU) or from the experimental evidence on the spacing of the normal compression lines (or the magnitude of wetting-induced collapse) (UNITN, GU and USTRAT) or by considering a combination of both of these two aspects of behaviour (ENPC and UNINA). Teams then selected a value for $N(0)$ to fix the locations of all the normal compression lines. In some cases this was done by simply matching the position of the saturated normal compression line, whereas other teams selected a value for $N(0)$ by a procedure which attempted to provide the best overall match to the positions of all normal compression lines.

Values of p^c and $N(0)$ determined by the different teams are listed in Table 2. It is not helpful to compare these values in isolation. For example, the value of p^c depends on the value already selected for the parameter r , with p^c extremely sensitive to r when the value of r is close to 1. As teams selected different values

for r , and many of these are close to 1, widely different values of p^c have been proposed. For values of r less than 1, a very low value of p^c is required (much lower than the range of \bar{p} over which the model is to be applied). Conversely, for values of r greater than 1, a very high value of p^c is required. In both cases, the required value of p^c becomes more extreme as r approaches 1 (e.g. GU). The required value of $N(0)$ then depends upon the value of p^c selected, because the intercept $N(s)$ of each normal compression line is defined at the reference pressure p^c (see Equations 3 and 4). Hence, given the widely different values of p^c selected by the different teams, significant variation in the values of $N(0)$ is only to be expected.

Predicted normal compression lines

Figure 6 shows the resulting normal compression lines predicted by the various teams at $s = 0$, $s = 20 \text{ kPa}$, $s = 150 \text{ kPa}$ and $s = 800 \text{ kPa}$. There are significant differences between the predictions of the different teams. This is very important, because these normal compression lines give both the magnitude of compression during isotropic loading at constant suction to virgin states and also the variation of potential wetting-induced collapse compression. Hence, the variation between the predictions of the different teams shown in Figure 6 is worrying.

Inspection of Figure 6 shows that UNINN predicted normal compression lines that converge significantly as \bar{p} increases (because their value for r is much greater than 1), whereas all other teams predicted normal compression lines that are approximately parallel (r values close to 1). Even for the 6 teams other than UNINN, there is however considerable variation between the predicted spacing of the normal compression lines for different values of suction.

The predicted spacing between the normal compression line at $s = 800 \text{ kPa}$ and the saturated normal compression line at $s = 0$ in Figure 6 is, in almost all cases, essentially dependent on the values of only r and p^c , because the predicted variation of $\lambda(s)$ with suction has essentially stopped by $s = 800 \text{ kPa}$ (see Figure 5) and any

dependency on the value of κ_s (through Equation 4) is very minor. An exception is ENPC, where the value of β also plays a part, because their very low value of β means that they predict $\lambda(s)$ still varying with s for suctions above 800kPa (see Figure 5). Inspection of Figure 6 and comparison with the experimental data shows that the spacing between the $s = 800$ kPa and $s = 0$ lines predicted by USTRAT is unrealistically small. This is because a much smaller value of p^c should have been used with their value of r (compare with the more realistic spacing of UNINA, who had a similar value of r but a much lower value of p^c , see Table 2). The same problem is apparent, to a lesser degree, for some other teams (e.g. UNITN). Conversely, the spacing between the $s = 800$ kPa and $s = 0$ lines predicted by UNINN over most of the range of \bar{p} of interest is unrealistically large, because a less extreme value of p^c should have been used with their very high value of r . Note that GU required a very extreme value for p^c in order to predict a realistic spacing between the $s = 800$ kPa and $s = 0$ lines, because they had a value of r closer to 1 than any other team (see Table 2).

The discussion above highlights the role of the parameter p^c in determining the spacing between normal compression lines for extreme values of suction (once the values of $\lambda(0)$ and r have been selected). Given the crucial importance of accurately capturing the spacing between normal compression lines for different values of suction, and the failure to achieve this by some teams (see Figure 6), an important conclusion to arise from the benchmarking exercise is that it is best to determine a value for p^c by a method that places the main emphasis on matching normal compression line spacing (rather than on attempting to match the initial shape of the LC yield curve).

The relative spacing of the normal compression lines for different values of suction in Figure 6 (i.e. where the lines for $s = 20$ kPa and $s = 150$ kPa fit between the lines for $s = 800$ kPa and $s = 0$) depends almost solely on the value of β (the elastic parameter κ_s also plays a role, through Equation 4, but this is very minor). DU and UNINA proposed relatively high values of β , and this means that in Figure 6 the $s = 150$ kPa line is indistinguishable from the $s = 800$ kPa line and even the

$s = 20 \text{ kPa}$ line is much closer to the $s = 800 \text{ kPa}$ line than to the $s = 0$ line. Conversely, ENPC proposed a low value of β , and this means that the $s = 20 \text{ kPa}$ line is indistinguishable from the $s = 0$ line and even the $s = 150 \text{ kPa}$ line is much closer to the $s = 0$ line than to the $s = 800 \text{ kPa}$ line. Other teams employed intermediate values of β . This included GU, who specifically used the experimental evidence on the relative spacing of the normal compression lines at different values of suction in determining a value for β .

Given the crucial importance of accurately capturing the spacing between normal compression lines for different values of suction, and the failure to achieve this by some teams (see Figure 6), the discussion above indicates that it will generally be best to determine a value for β by a method that places the main emphasis on matching the experimental relative spacing between normal compression lines for different values of suction (rather than on attempting to match the experimental variation of $\lambda(s)$). This is particularly important when the experimental values of $\lambda(s)$ cannot be well-matched by BBM (e.g. because they do not vary monotonically with suction), and hence differences of procedural detail may lead to widely different values of β if the methodology is based on attempting to match the experimental variation of $\lambda(s)$.

Strength parameters M and k and predicted critical state lines

Parameters M and k determine the positions in the $q: \bar{p}$ plane of critical state lines for different values of suction (see Equation 10). Each of the six triaxial tests involved constant suction shearing to a critical state (five at $s = 800 \text{ kPa}$ and one at $s = 20 \text{ kPa}$), and all teams used the experimental critical state values of q and \bar{p} from these tests to determine values for M and k (DU used only the data at $s = 800 \text{ kPa}$, whereas all remaining teams used all six experimental critical state data points). As a consequence, the values of M and k proposed by the various teams are all very consistent (see Table 2), with M in the range 1.12 to 1.18 and k generally in the range 0.41 to 0.50. The locations of the critical state lines in the $q: \bar{p}$ plane predicted by the various teams are therefore very similar (see Figure 7). A minor

discrepancy is that USTRAT proposed a significantly lower value of k ($k = 0.3$) than other teams, resulting in the prediction of lower critical state values of q than other teams at suctions greater than zero (see Figure 7).

Figure 8 shows the critical state lines in the $v: \ln \bar{p}$ plane predicted by the various teams (from Equation 11). As indicated by Equation 11, each critical state line is curved in the $v: \ln \bar{p}$ plane, with the exception of the saturated line at $s = 0$. Inspection of Figure 8 shows large differences between the predictions of the different teams. This is mainly attributable to differences in the predictions for the corresponding normal compression lines (see Figure 6). Comparison of Equation 11 with Equation 3 shows that the predicted spacing Δv between the critical state line for a given value of suction and the corresponding normal compression line varies with \bar{p} and is given by:

$$\Delta v = (\lambda(s) - \kappa) \ln \left(2 + \frac{ks}{\bar{p}} \right) \quad (12)$$

Teams generally proposed reasonably similar values of κ and k , and most teams (with the exception of UNINN) predict reasonably similar values of $\lambda(s)$ (see Figure 5). Hence, from Equation 12, the different teams predict reasonably similar variation with s and \bar{p} of the spacing between each critical state line and the corresponding normal compression line. This means that (with the exception of UNINN) teams predict reasonably similar reductions of v during constant suction shearing of a normally consolidated soil from the normal compression line to the critical state line (see later).

Initial value of $\bar{p}_0(0)$

The initial value of the hardening parameter $\bar{p}_0(0)$ defines the initial position of the LC yield surface in BBM. The initial shape of the LC yield curve in the $s: \bar{p}$ plane is then defined through Equation (6) by the values of p^c , κ and the parameters

defining the variation of $\lambda(s)$ with suction ($\lambda(0)$, r and β). Experimental values of yield stress under isotropic stress states (showing the initial form of the LC yield curve, and hence useful to the teams in determination of an initial value for $\bar{p}_0(0)$) were available at $s = 0$ (SAT-1) and $s = 800$ kPa (IS-NC-12 and IS-OC-06).

Table 2 shows that the initial values of $\bar{p}_0(0)$ proposed by the different teams ranged from 42 kPa to 291 kPa. The formal optimisation procedure employed by UNINN resulted in a lower value (42 kPa) than those determined by all other teams, and again comparison with the experimental results suggests that the procedure had failed to identify a true set of optimum parameter values. DU, GU and UNINA based their initial values of $\bar{p}_0(0)$ exclusively (or almost exclusively) on the yield point identified in the saturated test (SAT-1) and hence they all suggested similar values for $\bar{p}_0(0)$ (69 kPa to 85 kPa). As stated earlier, UNITN were unhappy about the consistency of the experimental results from SAT-1 and they therefore back-calculated their initial value of $\bar{p}_0(0)$ entirely from the yield stress measured in a test at $s = 800$ kPa (Test IS-OC-06), leading to a much higher initial value for $\bar{p}_0(0)$ (291 kPa). USTRAT and ENPC either took account of experimental yield points at both $s = 0$ and $s = 800$ kPa or attempted to best match patterns of collapse compression in Test TISO-1, and these approaches resulted in intermediate initial values of $\bar{p}_0(0)$ (120 kPa and 170 kPa).

Figure 9 shows the initial forms of the LC yield curve predicted by the different teams, with Figure 9(a) showing the predicted curves over the full experimental range of suction whereas Figure 9(b) shows an expanded view of the curves for low values of suction (up to $s = 100$ kPa). There are very significant differences between the forms of curve predicted by the various teams. These reflect the differences in the forms of normal compression lines predicted by the different teams (see Figure 6), because once the normal compression lines for different values of suction are defined (together with the values of the elastic parameters κ and κ_s) this fixes the form of the LC yield curve and how it develops during expansion.

Inspection of Figure 9(b) shows that the predicted yield stress at $s = 0$ varies from 42 kPa (UNINN) to 291 kPa (UNITN), directly reflecting the initial values of $\bar{p}_0(0)$ selected by the different teams. Inspection of Figure 9(b) shows that the predicted yield stress as suction tends to infinity varies from 193 kPa (USTRAT) to 1011 kPa (UNINN) and 1563 kPa (ENPC) (this limiting value predicted by ENPC is only approached at suctions considerably greater than the range shown in the figure). Consideration of the LC yield curve expression of Equation 6 shows that the predicted ratio of the yield stress at $s = \infty$ to the yield stress at $s = 0$, $\bar{p}_0(\infty)/\bar{p}_0(0)$, is a function mainly of the values of $\bar{p}_0(0)/p^c$ and r (with a small influence of the value of $\kappa/\lambda(0)$). The predicted ratio $\bar{p}_0(\infty)/\bar{p}_0(0)$ is largest for UNINN, because their proposed value of p^c is relatively extreme for their value of r (which is much greater than 1). In contrast, the ratio $\bar{p}_0(\infty)/\bar{p}_0(0)$ is smallest for USTRAT, because their proposed value of p^c is insufficiently extreme for their value of r (which is relatively close to 1).

Figure 9(a) illustrates that selection of a low value for β (e.g. ENPC) results in a yield curve shape where the yield stress \bar{p}_0 continues to vary significantly over a wide range of suctions. In contrast, selection of a high value for β (e.g. DU or UNINA) results in a yield curve shape where all significant variation of \bar{p}_0 occurs for suctions less than about 50 kPa.

RESULTS: SIMULATIONS OF SELECTED TESTS

The coordinating team from GU performed BBM simulations of all 9 experimental tests with the 7 different sets of parameter values shown in Table 2, as part of a process of investigating the implications of the differences in the parameter value sets proposed by the 7 contributing teams. Results of the simulations are shown here for 5 selected tests. When viewing these results it should be remembered that BBM was unable to provide a perfect match to all aspects of all 9 tests, and the challenge for the contributing teams was essentially one of trying to provide an adequate match to all 9 tests rather than a perfect match to any single test.

Saturated isotropic test SAT-1

Figure 10(a) shows the stress path for the saturated isotropic test SAT-1. Figure 10(b) shows the experimental results (in the $v : \ln p'$ plane) from the isotropic loading and unloading stages BCD, together with the corresponding model simulations using the 7 different parameter value sets.

Inspection of Figure 10(b) shows that all 7 teams predicted reasonably similar gradients for the saturated isotropic normal compression line ($\lambda(0)$) and for the pre-yield compression curve during loading and the swelling curve during unloading (κ) and that these all provided reasonable matches to the corresponding experimental gradients. There were however significant variations in the predictions of the yield stress during loading and the location of the saturated normal compression line, and in some cases the match to the experimental results was relatively poor.

The yield stress and the location of the saturated normal compression line in Test SAT-1 were well-matched by DU, GU and UNINA, as a consequence of the fact that these features were explicitly fitted in the parameter value selection procedures used by these teams. In contrast, the UNITN team explicitly ignored the results from Test SAT-1, because they considered them to be inconsistent with the results from the remaining tests, and as a consequence Figure 10(b) shows that they significantly overestimated the yield stress observed in this test and predicted that the saturated isotropic normal compression line was significantly above its observed position. This mis-match was linked to the fact that UNITN predicted the saturated isotropic normal compression line to be very close to the normal compression line for $s = 20$ kPa (see Figure 6(b)). The teams from ENPC and USTRAT also predicted that the saturated isotropic normal compression line was very close to the normal compression line for $s = 20$ kPa (see Figure 6(c) and Figure 6(g)), and as a consequence they too overestimated the yield stress in Test SAT-1 and predicted that the saturated isotropic normal compression line was above its observed position (see Figure 10(b)). Conversely, the parameter values proposed by UNINN, on the basis of their formal

optimisation procedure, resulted in the prediction of very wide spacing between the normal compression lines at different values of suction (see Figure 6(f)), and hence they underestimated the yield stress in Test SAT-1 and predicted that the saturated isotropic normal compression line was below its observed position (see Figure 10(b)).

Isotropic test TISO-1

Figure 11(a) shows the stress path for the suction-controlled isotropic test TISO-1. Figures 11(b) to 11(h) show the experimental results (in the $v : \ln \bar{p}$ plane) for all test stages and the corresponding 7 different model simulations. The experimental results appear to show elastic behaviour during initial loading stage AB, significant collapse compression during wetting stage BC, very small (elastic) shrinkage and swelling during drying stage CD and wetting stage FG respectively, yielding and plastic compression during loading stages DE and GH and elastic swelling during unloading stages EF and HI. All of this behaviour is qualitatively consistent with BBM.

Inspection of Figure 11(d) and Figure 11(f) shows that the predictions of ENPC and UNINA correctly include all qualitative elements of the observed behaviour, including elastic behaviour throughout loading stage AB, occurrence of collapse compression during wetting stage BC and occurrence of yielding and significant plastic compression during loading stages DE and GH. ENPC, however, over-predicts the magnitude of collapse compression during wetting stage BC and hence over-predicts the final volumetric strain at the end of the test, whereas UNINA under-predicts the magnitude of collapse compression during wetting stage BC and hence the final volumetric strain. This is because ENPC predicts an overly large spacing between the normal compression lines for $s = 800 \text{ kPa}$ and $s = 20 \text{ kPa}$ (see Figure 6(c)), whereas UNINA predicts a spacing between these normal compression lines that is too small (see Figure 6(e)). This difference is mainly attributable to the different values of β selected by ENPC and UNINA (0.0017 kPa^{-1} and 0.095 kPa^{-1} respectively).

Inspection of Figure 11(b) and Figure 11(h) shows that DU and USTRAT incorrectly predict that yielding would occur during the initial loading at a suction of 800 kPa (stage AB). This is attributable to the fact that the initial shape of the LC yield curve predicted by these two teams (USTRAT in particular) involves low values of yield stress at high suctions (see Figure 9(a)). In addition, DU under-predicts the magnitude of collapse compression during wetting stage BC and hence the final volumetric strain at the end of the test, as a consequence of under-predicting the spacing between the normal compression lines for $s = 800$ kPa and $s = 20$ kPa (largely due to the relatively high value of β proposed by DU). In contrast, USTRAT over-predicts the final volumetric strain at the end of the test, because the locations of the normal compression lines for all four experimental values of suction are poorly predicted.

Inspection of Figure 11(c) and Figure 11(e) shows that both UNITN and GU provide good matches to the magnitude of collapse compression during wetting stage BC and to the final volumetric strain at the end of the test, largely as a consequence of predicting an appropriate spacing between the normal compression lines for $s = 800$ kPa and $s = 20$ kPa (see Figure 6). However, both UNITN and GU incorrectly predict little or no plastic straining during loading stage DE at an intermediate suction of 150 kPa. This is because these two teams did not match well the experimental position of the normal compression line at $s = 150$ kPa. This illustrates the fact that with BBM it was impossible to match well the observed positions of the normal compression lines for all 4 experimental values of suction ($s = 0$ from Test SAT-1, $s = 20$ kPa and $s = 150$ kPa from Test TISO-1 and $s = 800$ kPa from triaxial tests IS-NC-12 and IS-OC-06). This was because the experimental results indicated large spacing between the $s = 0$ and $s = 20$ kPa lines, small spacing between the $s = 20$ kPa and $s = 150$ kPa lines, but then large spacing again between the $s = 150$ kPa and $s = 800$ kPa lines, and this type of irregular spacing could not be captured by BBM. Therefore, even if matching the positions of the normal compression lines was given over-riding priority in the parameter value selection procedure, it was at best only possible to match three of the four experimentally observed locations of normal compression lines. For example, GU placed great emphasis on matching normal compression line locations, but they explicitly chose to match well the normal

compression lines for $s = 0$, $s = 20$ kPa and $s = 800$ kPa, and accepted that this meant poor matching of the normal compression line for $s = 150$ kPa.

Inspection of Figure 11(g) shows that UNINN was another team who incorrectly predicted no plastic straining during loading stage DE at the intermediate suction of 150 kPa, but they also over-predicted both the magnitude of collapse compression during wetting stage BC and the final volumetric strain at the end of the test. This was a consequence of their formal optimisation procedure resulting in poor matching of the positions of normal compression lines for most values of suction.

Triaxial test IS-NC-12

Figure 12(a) shows the stress path for suction-controlled triaxial test IS-NC-12. Experimental results from the initial isotropic loading stage AB (at a suction of 800 kPa) are shown in Figure 12(b) (in the $v:\ln \bar{p}$ plane), together with the corresponding model simulations using the 7 parameter value sets. UNITN, ENPC, GU, UNINA and UNINN all provide satisfactory matching of the experimental results during initial isotropic loading, whereas DU and particularly USTRAT underestimate the yield stress and predict that the normal compression line for $s = 800$ kPa is below the observed position. This is attributable to the fact that the initial shape of the LC yield curve predicted by these two teams involves low values of yield stress at high suctions (see Figure 9(a)).

Figure 12(c) and Figure 12(d) show the experimental results and model predictions for the shearing stage BCDE, as plots of deviator stress q against axial strain ε_1 and volumetric strain ε_v against shear strain ε_s . The unload-reload loop has been omitted from the model predictions for clarity.

Inspection of Figure 12(c) shows that all teams predicted very similar values of final critical state deviator stress, as a consequence of selecting very similar values for the strength parameters M and k . These predictions of final critical state deviator stress are all good matches to the experimental result.

Figure 12(d) shows that 6 of the 7 teams predict fairly similar magnitudes of positive volumetric strain (compression) during shearing and that these predictions somewhat overestimate the compression observed in the experiment (DU provides the closest match). The reason that most of the teams predict similar magnitudes of compression during this drained shearing of a normally consolidated soil is that they predict very similar spacing between the normal compression line and the critical state line in the $v : \ln \bar{p}$ plane (see Equation 12). The exception is UNINN, who predict a much larger magnitude of compression than other teams during this shearing stage (see Figure 12(d)), because they have a much larger spacing between normal compression line and critical state line at a suction of 800 kPa than other teams, because they predict a much higher value of $\lambda(s)$ at $s = 800$ kPa than other teams (see Figure 5) and this has a crucial influence on Equation 12.

Returning to Figure 12(c), it can be seen that most teams significantly under-predict the development of axial strain at values of deviator stress less than the final critical state value, indicating that shear strains are under-predicted. Given that volumetric strains are somewhat over-predicted (see Figure 12(d)), the under-prediction of shear strains means that the flow rule of Equation 9 is not providing a good match to the experimental behaviour. This indicates a weakness of BBM, rather than a weakness of the parameter value selection procedures employed by the various teams. It should be noted that the form of the flow rule given by Equation 9, including the expression for α , was proposed by Alonso, Gens and Josa (1990) to match empirical experience of the value of K_0 for normally consolidated saturated soils, but this does not guarantee that Equation 9 matches observed behaviour when a soil is unsaturated or when the stress ratio corresponds to conditions other than one-dimensional straining. Inspection of Figure 12(c) shows that UNINN provides a better match than other teams to the experimentally observed development of axial strains prior to failure. This is, however, a consequence of two counter-acting errors: they substantially over-predict the volumetric strains (see Figure 12(d)) and when the inaccurate flow rule of Equation 12 is then applied to these volumetric strains this fortuitously results in prediction of shear strains which show a good match to the experimental results.

Triaxial test IWS-OC-01

Figure 13(a) presents the stress path for suction-controlled triaxial test IWS-OC-01, showing a wetting-drying cycle BCD (down to a suction of 10 kPa) prior to final shearing at a suction of 800 kPa. This represents shearing of an overconsolidated sample, where the overconsolidation has been produced by the previous wetting-drying cycle (the wetting leads to expansion of the yield surface). Experimental results from the shearing stage DEFGHI are shown in Figure 13(b) (in the $q : \varepsilon_1$ plane) and Figure 13(c) (in the $\varepsilon_v : \varepsilon_s$ plane), together with the corresponding model predictions. The two unload-reload loops have been omitted from the model predictions for clarity.

Figure 13(a) and Figure 13(b) show that the model simulations divide into two groups. DU, UNITN, UNINA and USTRAT predict yielding on the wet side of critical state for this overconsolidated sample, and hence they predict no occurrence of a peak deviator stress prior to reaching a critical state (Figure 13(b)) and positive volumetric strain (compression) during shearing (Figure 13(c)). In contrast, ENPC, GU and UNINN predict yielding on the dry side of critical state, and hence they predict a peak deviator stress and then post-peak softening to a critical state (Figure 13(b)) as well as negative volumetric strain (dilation) during shearing (Figure 13(c)). This difference is caused by the fact that the expanded shape of the LC yield surface after wetting to $s = 10$ kPa (with $\bar{p} = 600$ kPa) varies significantly between the different teams. In particular, ENPC, GU and UNINN predict that, after wetting-induced expansion, the cross-section of the yield surface at $s = 800$ kPa is considerably larger than predicted by the other 4 teams. Inspection of Figure 13(b) shows that the $q : \varepsilon_1$ simulations of those teams who predict yielding on the wet side of critical state are much closer to the experimentally observed behaviour than those of the teams who predict yielding on the dry side. In terms of volumetric strains (Figure 13(c)), the experimental results show initial compression during shearing and then dilation, with the magnitude of final dilation being substantially greater than predicted by even the 3 teams who show yielding on the dry side.

Oedometer test EDO-1

Figure 14(a) shows the stress path for the suction-controlled oedometer test EDO-1 in a plot of suction against vertical net stress $\bar{\sigma}_v$. The experimental stress path in the $q:\bar{p}$ plane is unknown, because there were no experimental measurements of horizontal stress.

The variation of horizontal net stress in an oedometer test is determined by the zero lateral strain condition and is therefore influenced by the material behaviour. As a consequence, each of the 7 different model simulations of oedometer test EDO-1 (each with a different parameter value set) shows a different predicted variation of horizontal net stress and hence a different stress path in the $q:\bar{p}$ plane. Figure 14(b) shows the predicted stress path in the $q:\bar{p}$ plane using the parameter value set proposed by ENPC. The stress paths predicted by other teams showed significantly different values of stress, but common qualitative features.

Inspection of Figure 14(b) shows that each of the loading stages AB, DE and GH involves an initial elastic section of stress path and then a yield point followed by an elasto-plastic section of stress path. The gradient of the elastic sections varies with \bar{p} (and, to a lesser extent, specific volume v), because of the assumption of a constant elastic shear modulus G (Equation 2) in combination with a variable elastic bulk modulus K (through Equation 1). For example, the initial elastic section of stress path AB has a very steep gradient in the $q:\bar{p}$ plot, whereas the initial elastic section of stress path GH has a much shallower gradient (see Figure 14(b)). The subsequent elasto-plastic sections of the stress paths for loading stages AB, DE and GH each initially traverses around the yield curve (with only modest expansion of the curve), until the stress ratio $q/(\bar{p} + ks)$ approaches the appropriate value corresponding to one-dimensional elasto-plastic straining. The assumption of a constant value of elastic shear modulus G can result in a predicted gradient for an elastic section of stress path that is rather unrealistic (for example, the very steep initial elastic section of stress path AB shown in Figure 14(b)) and hence unrealistic prediction of where the stress path will arrive at the yield surface.

The stress paths for unloading stages EF and HI in Figure 14(b) are both entirely elastic. Finally, the stress paths for wetting stages BC and FG and drying stage CD all have a gradient of $-3/2$ in the $q:\bar{p}$ plane (see Figure 14(b)), simply as a consequence of the fact that vertical net stress $\bar{\sigma}_v$ was constant during these stages.

Figure 15 shows the experimental results of oedometer test EDO-1 in the $v:\ln\bar{\sigma}_v$ plane, together with the 7 different model predictions. Features of the experimental results in Figure 15 include collapse compression during wetting stage BC and elasto-plastic compression during loading stages DE and GH. Almost all the teams made no use of the oedometer test results in their parameter value selection procedures, because the predicted stress path for the oedometer test was both highly complex and also impossible to specify precisely until the model parameter values were selected.

The model simulations in Figure 15 predict the qualitative behaviour with varying degrees of success, but all model simulations show significant errors in the magnitude of predicted volumetric strain during at least one stage, and the final volumetric strain by the end of the test is poorly predicted by most teams. The model predictions for the oedometer test generally show significantly poorer matches with the experimental results than those for the isotropic tests and triaxial tests. This can be partly attributed to the fact that the oedometer test results were not used in the process of determining parameter values. An additional factor, however, is that the predicted response during suction-controlled oedometer tests is even more sensitive to the material behaviour than that during isotropic or triaxial tests, because even the stress path followed is strongly influenced by the material behaviour.

RESULTS: OTHER IMPLICATIONS

The results presented above demonstrate that the 7 different BBM parameter value sets proposed by the various teams result in some significant differences in predicted behaviour even for the 9 laboratory tests used in the process of determining parameter values. It was considered likely that differences in predictions would be even greater

during blind predictions of other stress or strain paths (as would occur, for example, during application of BBM in numerical modelling of a boundary value problem). This issue was explored by the coordinating team from GU, who simulated various fictitious stress paths with the 7 different parameter value sets and also investigated other aspects of predicted behaviour. Two of these aspects are presented here for illustration.

Predicted development of LC yield curve shape during expansion

Figure 9 already demonstrated that the parameter value sets proposed by the 7 teams resulted in very significant differences in the predictions of initial shape and position of the LC yield curve. Figure 16 illustrates how these differences in yield curve shape develop as the LC yield curve expands. Figure 16(a) shows the LC yield curve shape predicted by each of the 7 teams when a common value of saturated isotropic yield stress $\bar{p}_0(0)=120$ kPa is assumed in all cases (corresponding approximately to the average initial value of $\bar{p}_0(0)$ proposed by the teams). Figure 16(b) shows the development of LC yield curve shape after expansion to $\bar{p}_0(0)=500$ kPa .

The shape of the LC yield curve determines, amongst other things, whether collapse compression will occur during a given wetting path and the value of suction at which this collapse compression will commence. Figures 16(a) and 16(b) show that the 7 different parameter value sets proposed by the 7 teams will inevitably lead to very different predictions of volume change during wetting, and that these differences will remain large even after expansion of the LC yield curve.

Closer inspection of Figures 16(a) and 16(b) also shows that the relative positions of the LC yield curve predicted by the different teams can change during expansion. For example, in Figure 16(a) the yield stress predicted at a suction of 800 kPa is largest for UNINN, followed by GU, UNINA and DU in sequence, whereas in Figure 16(b) the order has changed to UNINA followed by GU, DU and UNINN in sequence. Further changes of order occur as the yield curve is expanded to even higher values of

$\bar{p}_0(0)$. This indicates that, amongst other things, differences in predicted behaviour during wetting will not remain constant for all wetting paths and all stress histories.

Predicted behaviour during wetting

Differences in predicted behaviour during wetting are explored further in Figure 17. This figure shows the predicted variation of specific volume v during wetting paths from $s = 800$ kPa to $s = 0$ under an isotropic stress state conducted at $\bar{p} = 100$ kPa (Figure 17(a)), $\bar{p} = 200$ kPa (Figure 17(b)) or $\bar{p} = 500$ kPa (Figure 17(c)). Each part of the figure should be read from right to left, as suction is reduced during a wetting path. The predictions shown in Figure 17 are for the 7 different parameter value sets, including the 7 different initial values of $\bar{p}_0(0)$, and with a previous history consisting of simple isotropic loading at $s = 800$ kPa to the start of the wetting path.

In Figure 17(a) all predictions show elastic swelling through the majority of the wetting path, because the initial stress state at $\bar{p} = 100$ kPa , $s = 800$ kPa is inside the initial location of the LC yield curve in all cases (see Figure 9(a)). UNITN, ENPC and USTRAT predict that swelling continues throughout the entire wetting path, with the wetting path remaining inside the LC yield curve (see Figure 9(b)), because these 3 teams proposed initial values of $\bar{p}_0(0)$ larger than 100 kPa (see Table 2). In contrast, close inspection of Figure 17(a) shows that the other 4 teams predict varying amounts of collapse compression in the very last part of the wetting path as the LC yield curve is reached (see Figure 9(b)), because these 4 teams proposed initial values of $\bar{p}_0(0)$ less than 100 kPa (see Table 2).

In Figure 17(b), where the wetting takes place at $\bar{p} = 200$ kPa , UNINN is now the only team that predicts swelling throughout the entire wetting path, because they are the only team that proposed an initial value of $\bar{p}_0(0)$ larger than 200 kPa (see Table 2) and hence they are the only team to predict that the LC yield curve is not reached during wetting. At the opposite extreme, USTRAT predicts that the stress state will be already on the LC yield curve at the start of wetting, because they predict an initial

location of the yield curve with a yield stress \bar{p}_0 less than 200 kPa when the suction is 800 kPa (see Figure 9). USTRAT therefore predict that plastic volumetric strains will occur throughout the entire wetting process. However, during the early part of wetting the predicted magnitude of positive plastic volumetric strain (collapse compression) is less than the magnitude of negative elastic volumetric strain (elastic swelling) and hence the collapse compression is hidden and a net swelling response is predicted (see Figure 17(b)). The small magnitude of positive plastic volumetric strains predicted during the early part of wetting is a consequence of the very steep gradient of the LC yield curve at these higher values of suction (see Figure 9(a)). As the suction is reduced (and the LC yield curve becomes less steep), USTRAT predicts that the magnitude of plastic volumetric strain increments gradually increases and the overall response gradually changes from swelling to collapse compression, with no sudden change of behaviour (see Figure 17(b)). In contrast, ENPC, UNINN, GU, UNINA and DU predict that, when the wetting takes place at $\bar{p} = 200$ kPa, the LC yield curve will be reached late in the wetting process (see Figure 9), when the LC yield curve is not very steep, and hence a sudden change from swelling (elastic behaviour) to collapse compression (plastic behaviour) is predicted late in the wetting path (see Figure 17(b)).

Figure 17(c) shows that when wetting takes place at $\bar{p} = 500$ kPa all teams predict that collapse compression will occur in the later part of wetting, but there are major differences in the predictions of the final magnitude of collapse compression and the value of suction at which collapse compression commences. USTRAT and DU predict that plastic volumetric strains will occur throughout the entire wetting process, but with the magnitude of plastic volumetric strain increments initially very small, so that the overall response shows a gradual change from swelling to collapse compression. For DU this transition occurs only very late in the wetting process, because the very high value of β that they propose (see Table 2) means that they predict that the LC yield curve remains very steep to suctions less than 50 kPa (see Figure 9). ENPC predict that the LC yield curve is reached at a relatively high value of suction, in excess of 400 kPa, but at this point a sharp transition to overall collapse compression is predicted, because the high value of β that they propose (see Table 2) means that they predict that the LC yield curve is not very steep even at suctions in

excess of 400 kPa (see Figure 9(a)). Finally, UNITN, UNINN, GU and UNINA predict that the LC yield curve is reached late in the wetting process, at a relatively low value of suction (see Figure 9(b)), when the LC yield curve is not very steep, and hence they all predict a sharp transition from swelling to collapse compression late in the wetting process (see Figure 17(c)).

Figures 17(a), 17(b) and 17(c) illustrate that the 7 different parameter value sets proposed by the various teams result in substantially different predictions of volumetric strains during wetting, whatever the value of mean net stress. This is a matter of considerable concern, given that wetting-induced volumetric strains are often one of the most crucial aspects of mechanical behaviour of unsaturated soils.

CONCLUSIONS

All teams were provided with the experimental results from 9 tests performed on compacted samples of a soil from the campus of UPC Barcelona. Each of the 7 participating teams used the experimental results to determine values for the ten BBM soil constants (κ , κ_s , G , $\lambda(0)$, r , β , p^c , $N(0)$, M and k) and an initial value for the hardening parameter $\bar{p}_0(0)$. The BBM was unable to match perfectly the experimental data, and there was therefore no single “correct” answer for the set of parameter values. Hence it was inevitable that there would be differences in the parameter values derived by the various teams, as a consequence of differences in the procedures used to determine parameter values and variation of emphasis given to different aspects of the experimental results. It was, however, notable that the values proposed for some parameters varied very substantially between the 7 teams.

Determination of values for the elastic parameters κ , κ_s and G and the strength parameters M and k is generally relatively straightforward and non-controversial. The values of M and k proposed by the 7 teams showed very little variation. There was more variation in the proposed values of the elastic parameters κ , κ_s and G , but the differences were generally relatively unimportant in terms of the overall soil

behaviour and were explainable in terms of differences of procedural detail between the 7 teams.

The major challenge in determining BBM parameter values from experimental data is selection of values for the constants $\lambda(0)$, r , β , $N(0)$ and p^c and an initial value for the hardening parameter $\bar{p}_0(0)$. The values of these parameters control the predicted gradients and positions of normal compression lines for different values of suction, together with the predicted initial position and shape of the LC yield curve and how this shape develops during any subsequent expansion of the yield curve. Hence the values of these parameters control important aspects of predicted soil behaviour, such as whether collapse compression is predicted during a given wetting path and the predicted magnitude of any collapse compression. Crucially, many of these parameters influence several different aspects of predicted behaviour, making it difficult to achieve objective determination of parameter values. The challenge will be particularly difficult if the experimental variation of normal compression line gradient $\lambda(s)$ with suction or the experimental spacing of the different normal compression lines cannot be well matched by the BBM, for example if the experimental values of $\lambda(s)$ do not vary monotonically with suction or the spacings between the normal compression lines for different values of suction vary in an irregular fashion (both of these features were present in the experimental data used in this benchmarking exercise).

The proposals of the various teams for the values of $\lambda(0)$, r , β , p^c and $N(0)$ and the initial value of $\bar{p}_0(0)$ show some major variations, resulting in substantial differences for the predicted forms of the normal compression lines for different values of suction and for the initial form of the LC yield curve and how this develops as it expands. Given the crucial importance of these aspects of the BBM, these substantial differences between the proposals of the various teams indicate a worrying lack of reliability and robustness in the type of procedures generally used for selection of BBM parameter values. For example, the parameter value sets proposed by the different teams often result in very different predictions of volumetric strain during wetting (see Figure 17).

Some significant lessons for improvements in procedures for determining BBM parameter values from experimental data have emerged from the benchmarking exercise. Perhaps the most important lesson is to give considerable weight to matching as well as possible the experimental spacing between normal compression lines for different values of suction when determining values for the BBM parameters β and p^c . Gallipoli et al. (2010) suggest a formal method for selecting the value of β based on matching as well as possible the relative spacing between normal compression lines at different values of suction (where the normal compression lines for intermediate values of suction fall relative to the normal compression lines for extreme values of suction). This will generally be preferable to determining a value for β by attempting to match the experimental variation of $\lambda(s)$ with suction. If the value of β is determined in this way, the values of $\lambda(0)$ and r can then be selected to optimise the fit to the experimental variation of $\lambda(s)$ with suction, and then the value of p^c can be selected to optimise the match to the experimental absolute spacings of the normal compression lines for different values of suction over the experimental range of \bar{p} . Finally, the value of $N(0)$ can be selected to optimise the match to the actual positions of the normal compression lines in the $v : \ln \bar{p}$ plane. A formal approach following this logic is fully set out in Gallipoli et al. (2010) (the method of Gallipoli et al. (2010) was only developed after the benchmarking exercise described in this current paper, largely as a result of the outcome of the exercise).

Depending upon the particular application that the BBM will be used for (i.e. the nature of the boundary value problem that will be simulated and which aspects of the simulation results are considered most important), and also depending upon the nature of the experimental data that are available to determine BBM parameter values, it may also be useful to check whether the initial shape of the LC yield curve can be well-captured with the values of β , $\lambda(0)$, r and p^c determined from the normal compression lines as described above. If the initial shape of the LC yield curve is not well-captured, it may be appropriate to adjust the values of these four parameters with some form of iterative procedure, but this will often not be justified, because of the lack of precision with which yield stresses can be determined.

Unlike the other 6 teams, UNINN determined values for the majority of BBM parameters in a single formal optimization exercise based on inverse analysis. Comparison of BBM simulations with experimental results suggests that this formal optimization procedure was not successful in identifying a global minimum for the objective function, and instead converged on an inappropriate local minimum, resulting in a poor selection of parameter values. Although this does not mean that global optimization procedures of this type should never be used to determine BBM parameter values, it does emphasize that they should be used only with great caution and, at the very least, the predicted positions of normal compression lines for different values of suction should be checked against the corresponding experimental results.

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TABLES

Test	Typology	Do (mm)	Ho (mm)	e _o	S _{ro} (%)
SAT-1	saturated isotropic test	35	70	0.645	0.460
TISO-1	suction controlled isotropic test	38	76	0.627	0.480
IS-OC-03	suction controlled consolidated triaxial test	38	76	0.625	0.477
IS-NC-06	suction controlled consolidated triaxial test	38	76	0.623	0.479
IS-NC-12	suction controlled consolidated triaxial test	38	76	0.629	0.474
IS-OC-06	suction controlled consolidated unloaded triaxial test	38	76	0.629	0.474
IWS-OC-01	suction controlled consolidated wetted dried triaxial test	38	76	0.624	0.478
IWS-NC-02	suction controlled consolidated wetted triaxial test	38	76	0.644	0.463
EDO-1	suction controlled oedometric test	50	20	0.680	0.430

Table 1 Initial diameter (Do), height (Ho), void ratio (e_o) and degree of saturation (S_{ro}) of samples (after compaction).

Aspect of soil behaviour	Parameter	DU	UNITN	ENPC	GU	UNINA	UNINN	USTRAT
Elastic behaviour	κ	0.012	0.0104	0.007	0.0097	0.007	0.0098	0.0076
	κ_s	0.001	0.0021	0.002	0.0045	0.002	0.0035	0.0005
	G (MPa)	150	140	122	167	200	80	120
Plastic compressibility	$\lambda(0)$	0.074	0.097	0.072	0.078	0.072	0.072	0.08
	B (kPa ⁻¹)	0.125	0.0144	0.0017	0.0396	0.095	0.0222	0.008
	r	0.8	0.8293	0.8	1.0567	0.875	1.814	0.87
Other aspects of soil behaviour	N(0)	2	2.0375	2.17	1.4786	2.59	1.158	1.85
	p ^c (kPa)	0.5	4	0.07	2 · 10 ¹⁹	0.0001	29673	7
Strength behaviour	M	1.14	1.1333	1.13	1.1784	1.119	1.16	1.165
	k	0.46	0.449	0.45	0.4208	0.495	0.41	0.3
Initial state	Initial value of p(0) (kPa)	85	291	170	70	69	41.866	120

Table 2 BBM parameter values determined by each team

FIGURES

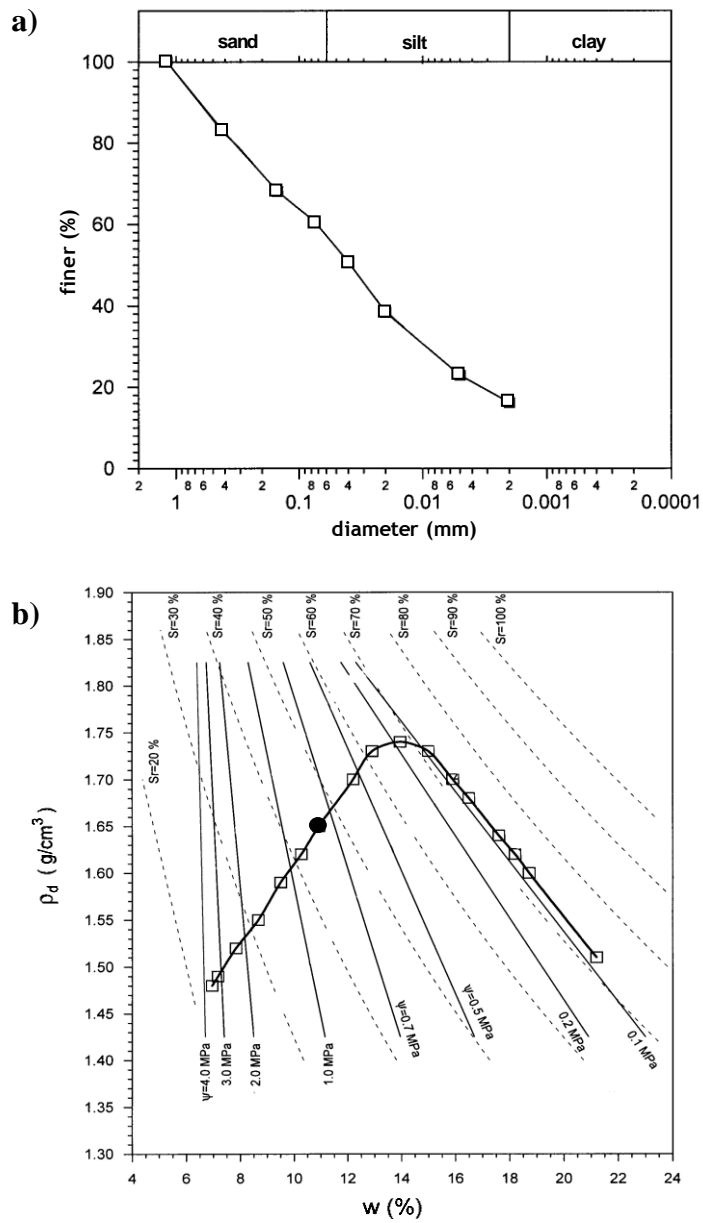


Fig. 1. (a) Particle size distribution; (b) compaction curve.

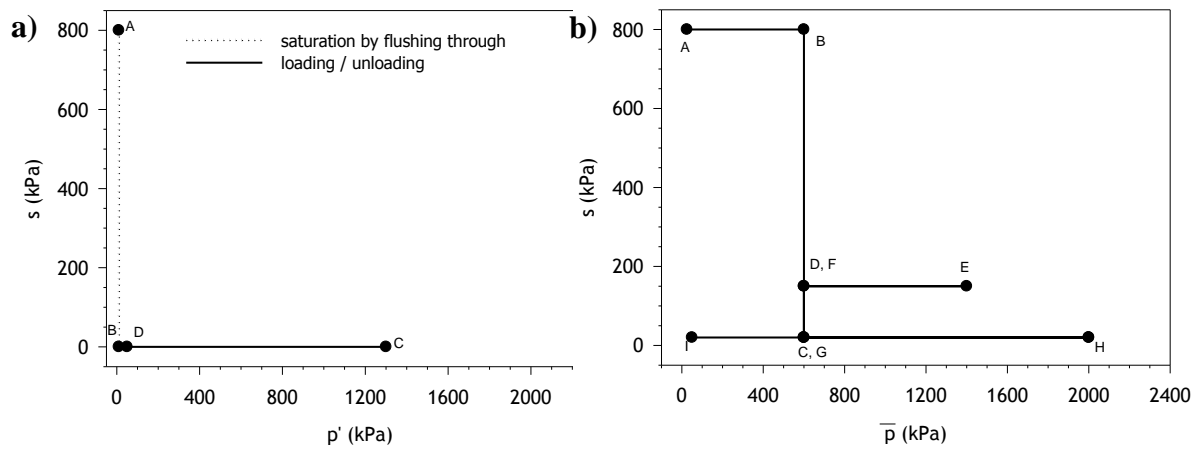


Fig. 2. Stress paths for isotropic tests: (a) saturated test SAT-1; (b) suction-controlled test TISO-1.

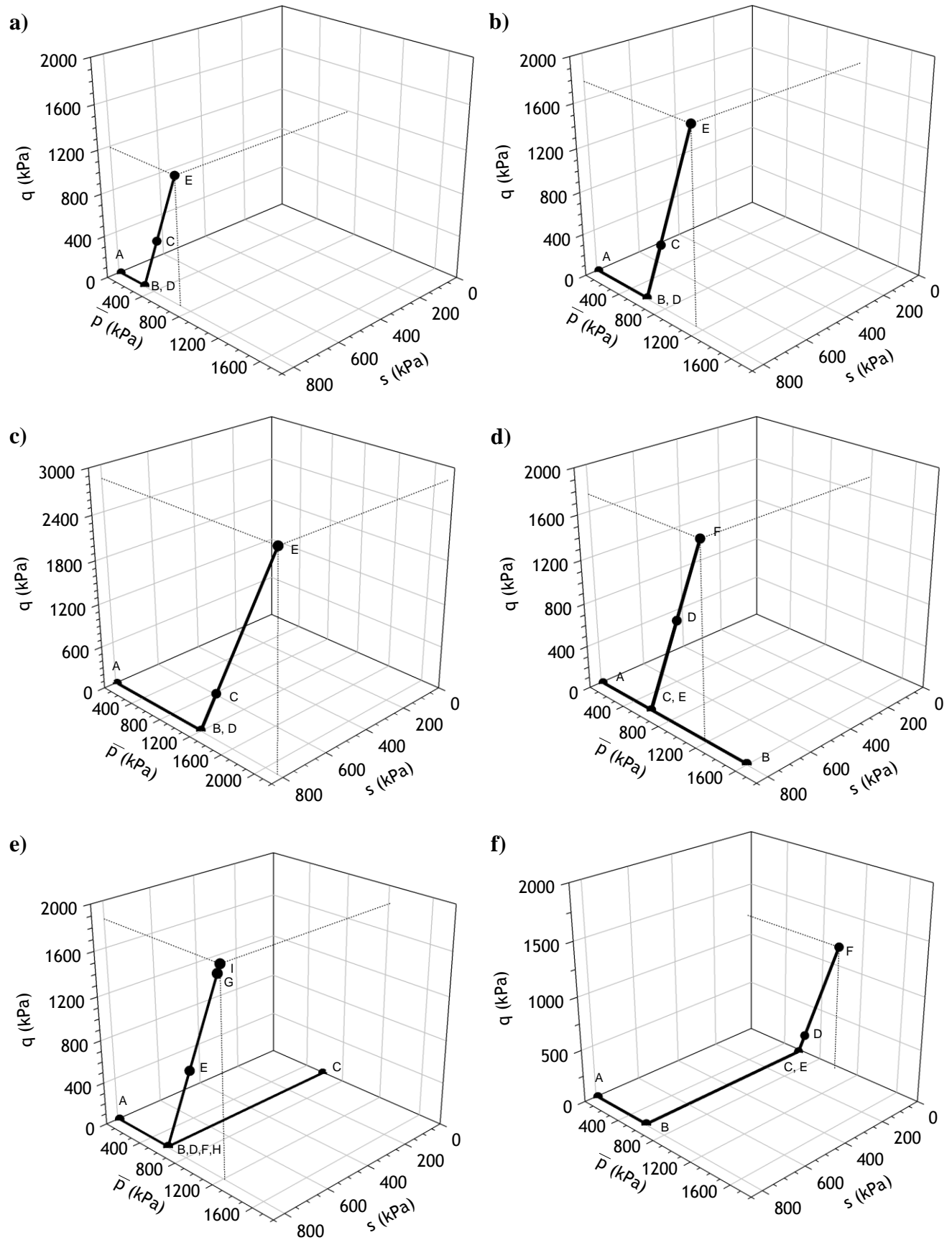


Fig. 3. Stress paths for suction-controlled triaxial tests: (a) IS-OC-03; (b) IS-NC-06; (c) IS-NC-12; (d) IS-OC-06; (e) IWS-OC-01; (f) IWS-NC-02.

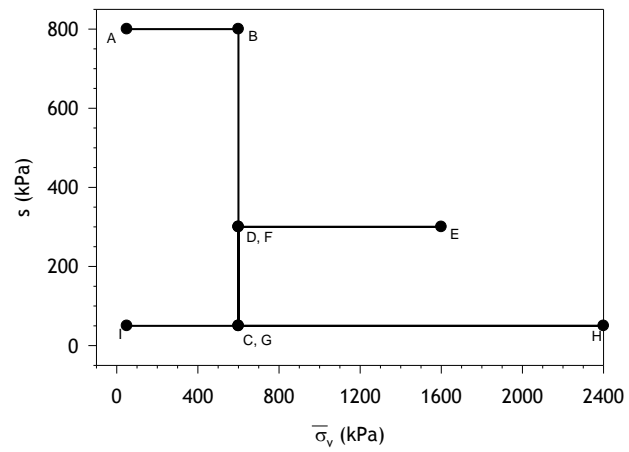


Fig. 4. Stress path for suction-controlled oedometer test EDO-1.

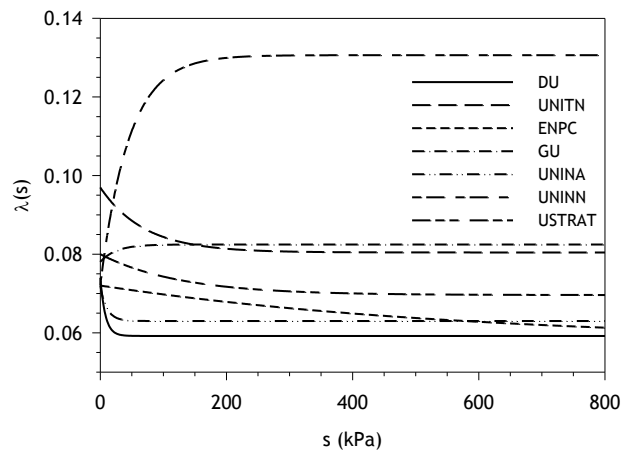


Fig. 5. Predicted variation of $\lambda(s)$ with suction.

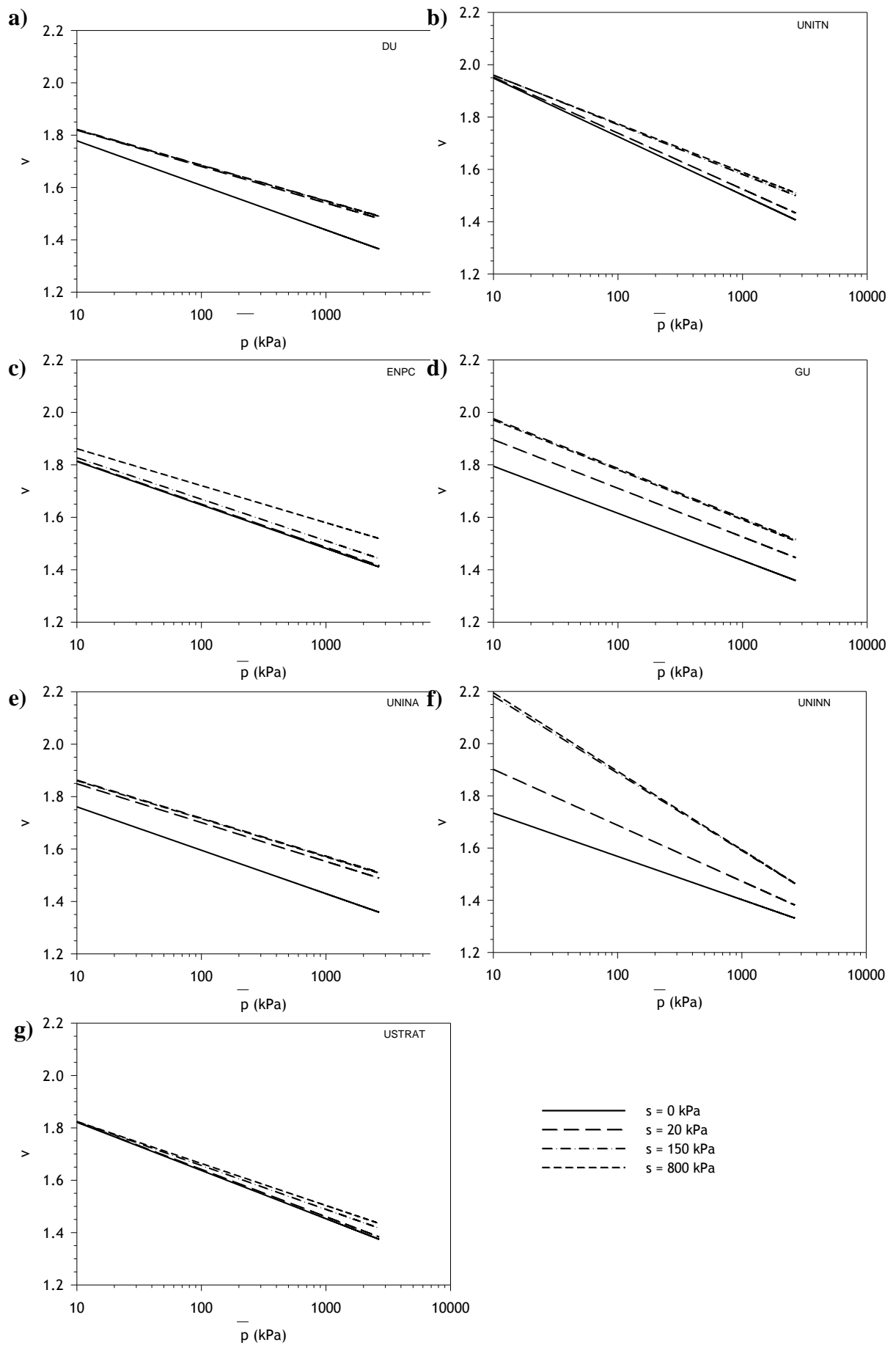


Fig. 6. Predicted normal compression lines for different values of suction.

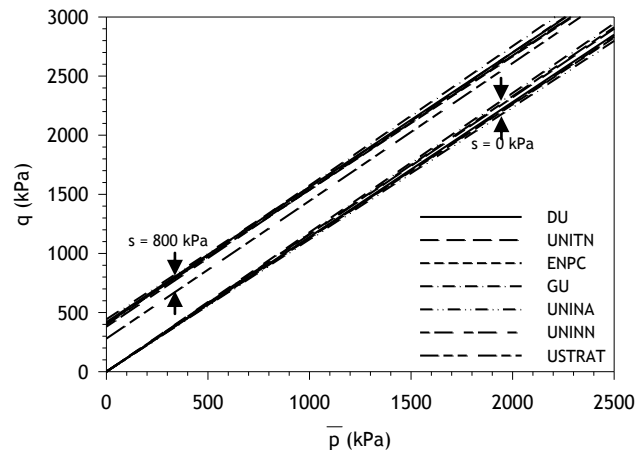


Fig. 7. Predicted critical state lines for suctions of 0 and 800 kPa in $q - \bar{p}$ plane.

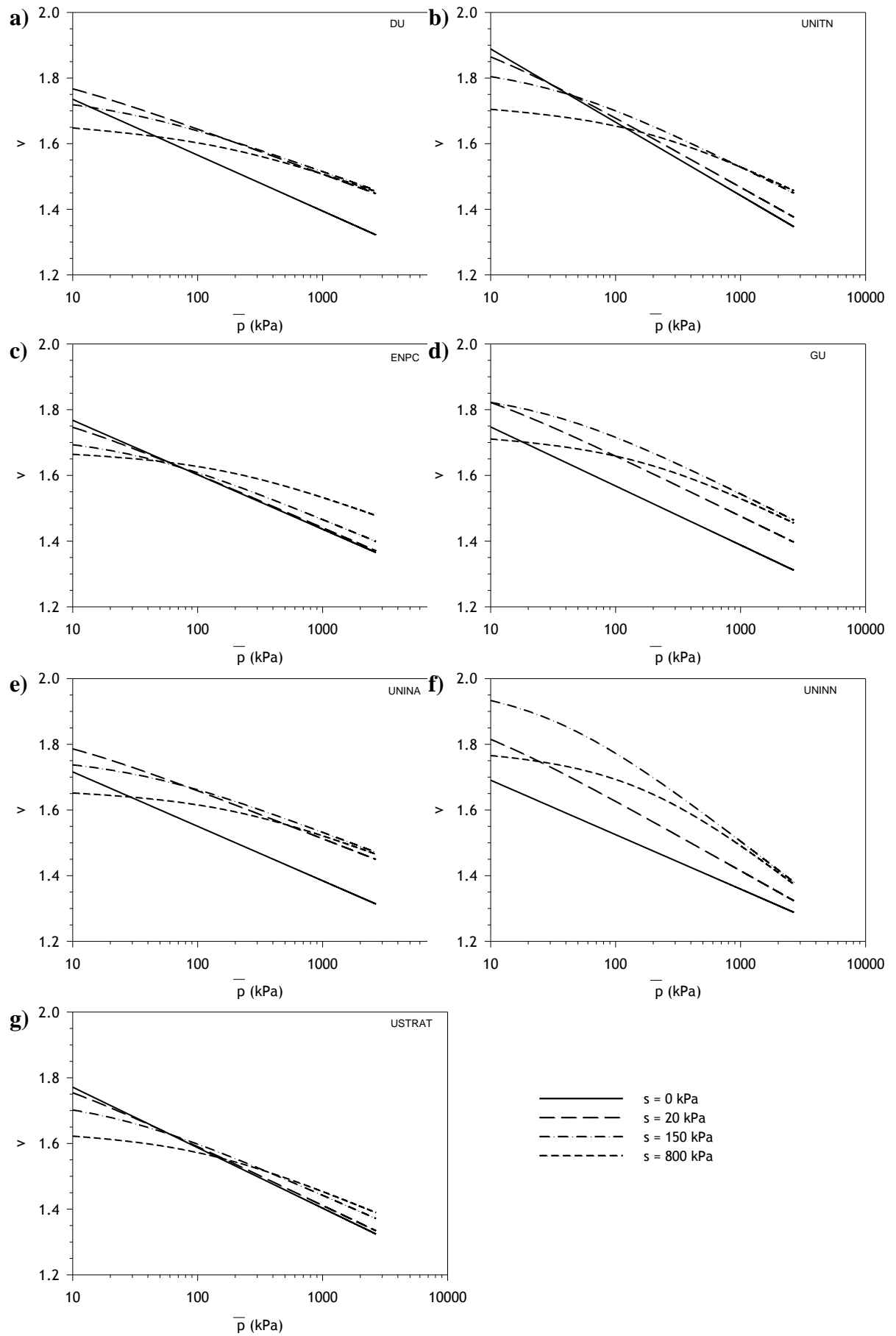


Fig. 8. Predicted critical state lines for different values of suctions in $\bar{v} : \ln \bar{p}$ plane.

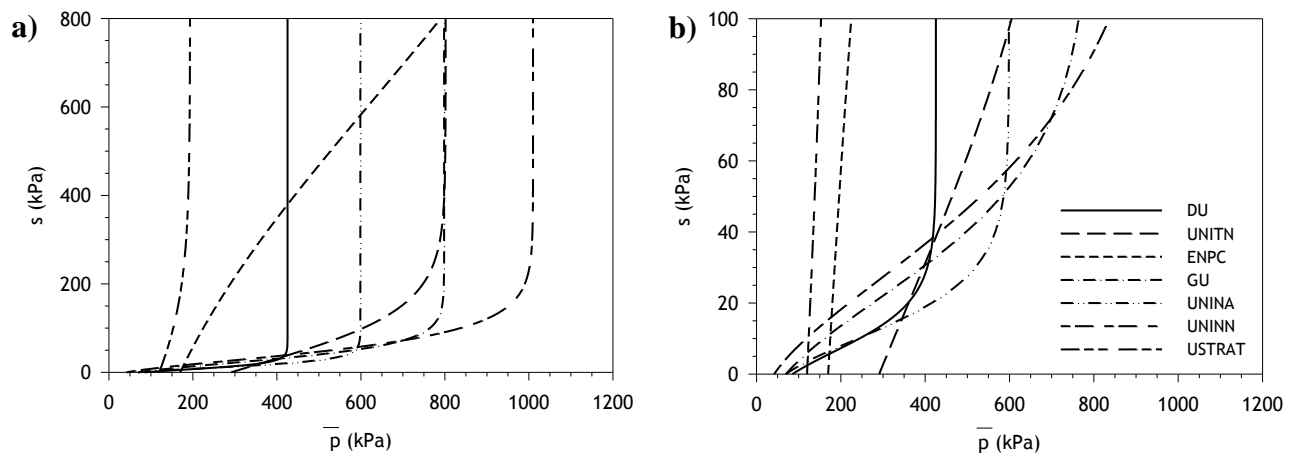


Fig. 9. Initial form of LC yield curve predicted by different teams: (a) full suction range; (b) magnified view of low suction range.

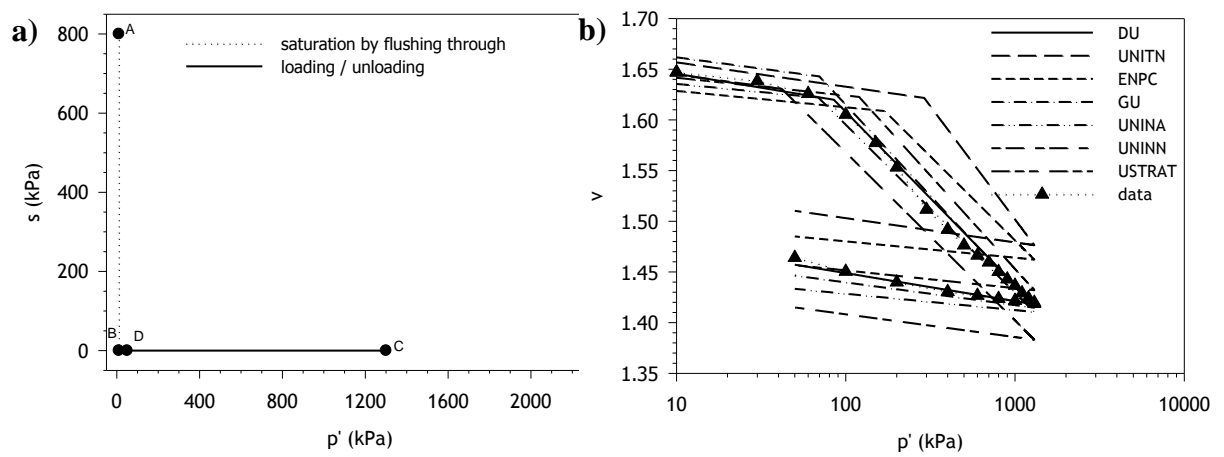


Fig. 10. Saturated isotropic test SAT-1: (a) stress path; (b) simulations and experimental data.

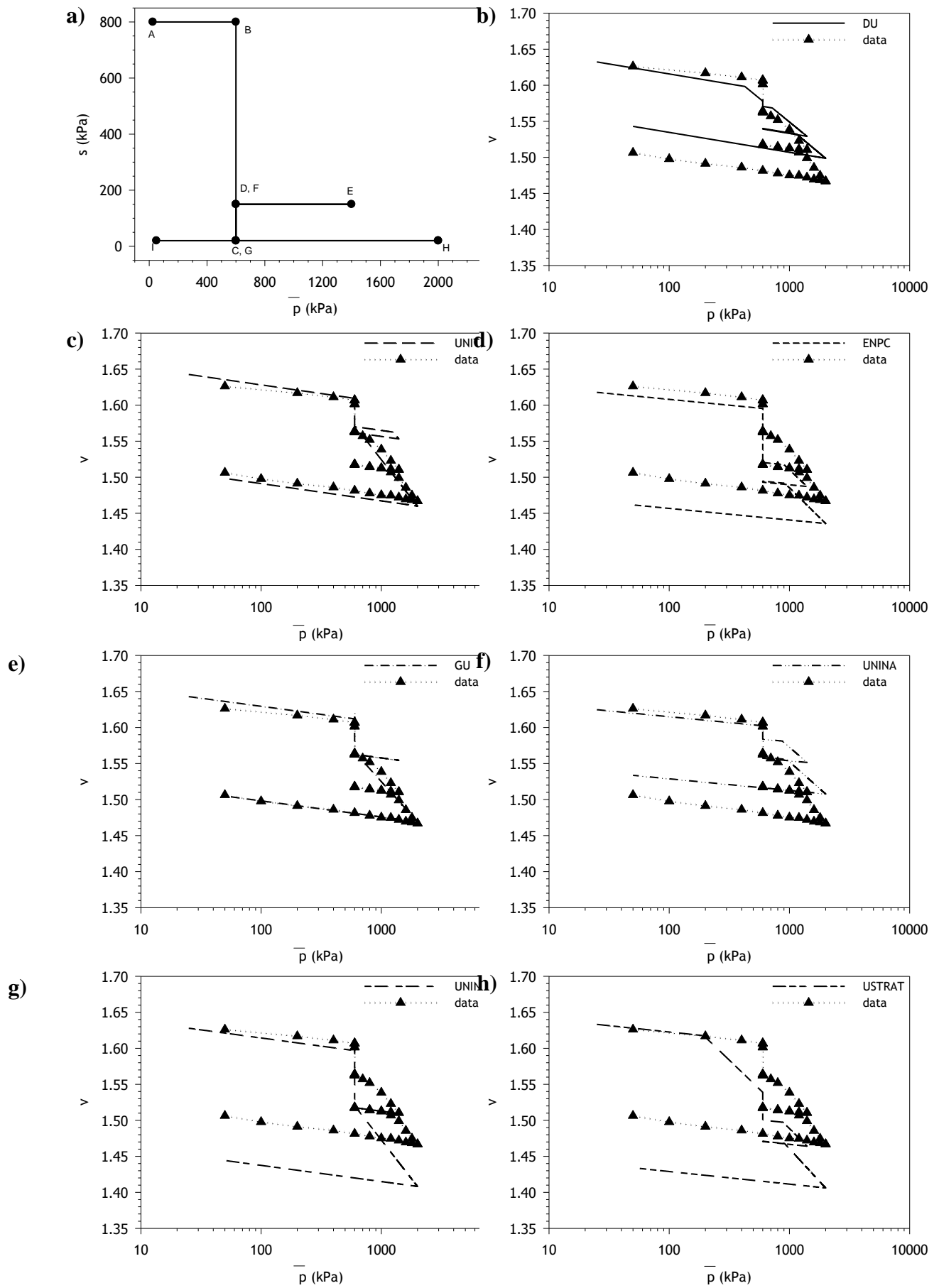


Fig. 11. Suction-controlled isotropic test TISO-1: (a) stress path; (b)-(h) simulations and

experimental data.

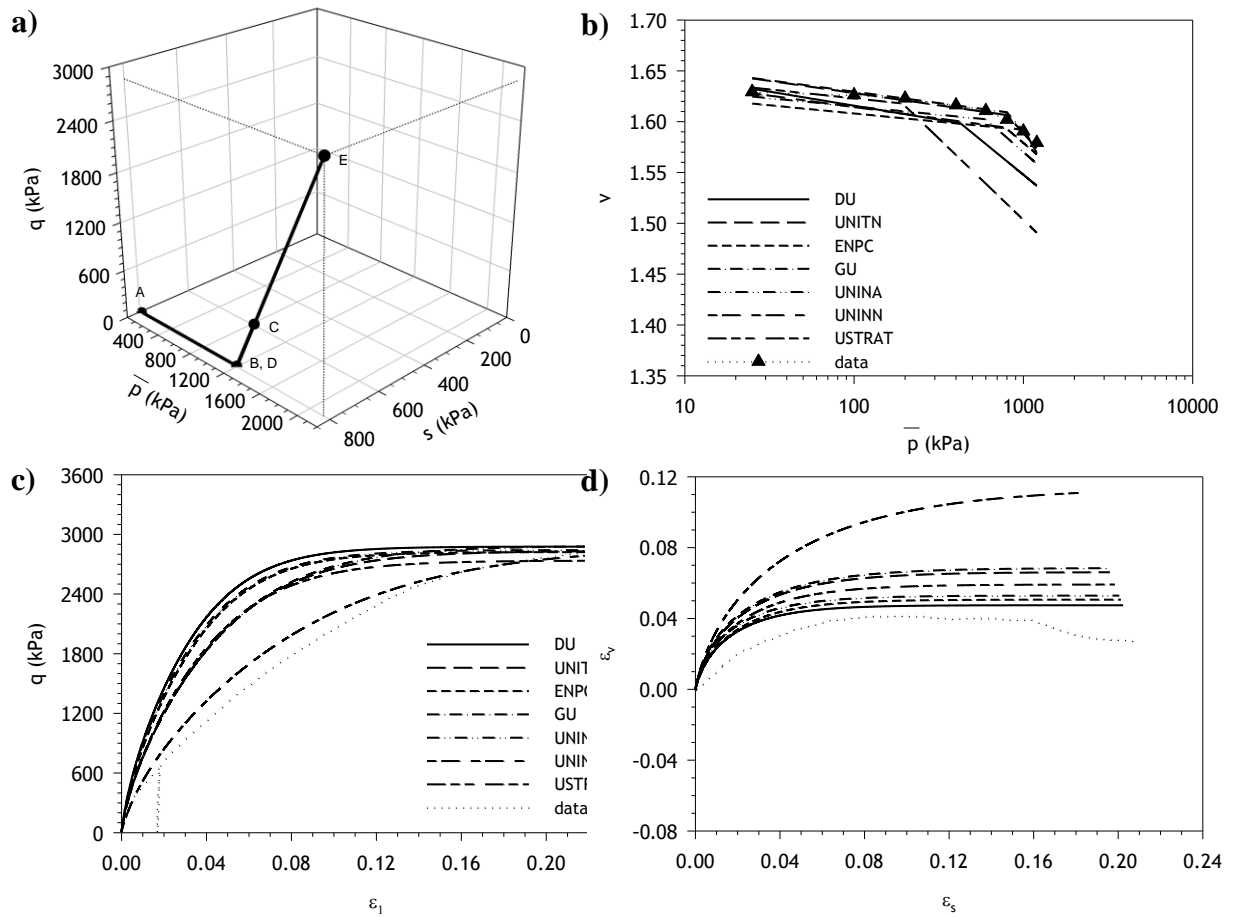


Fig. 12. Suction-controlled triaxial test IS-NC-12: (a) stress path; (b) simulations and experimental data for isotropic loading stage AB; (c,d) simulations and experimental data for shearing stage B-E.

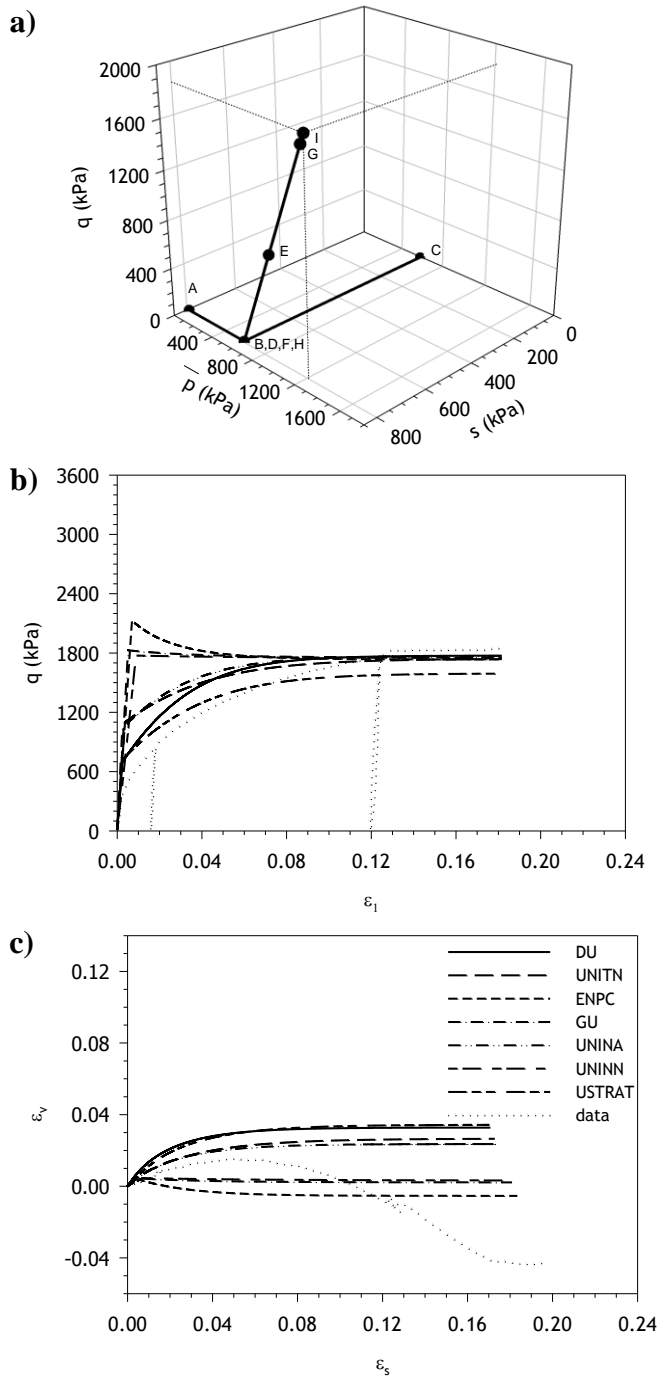


Fig. 13. Suction-controlled triaxial test IWS-OC-01:
(a) stress path; (b,c) Simulations and experimental
data for shearing stage D-I.

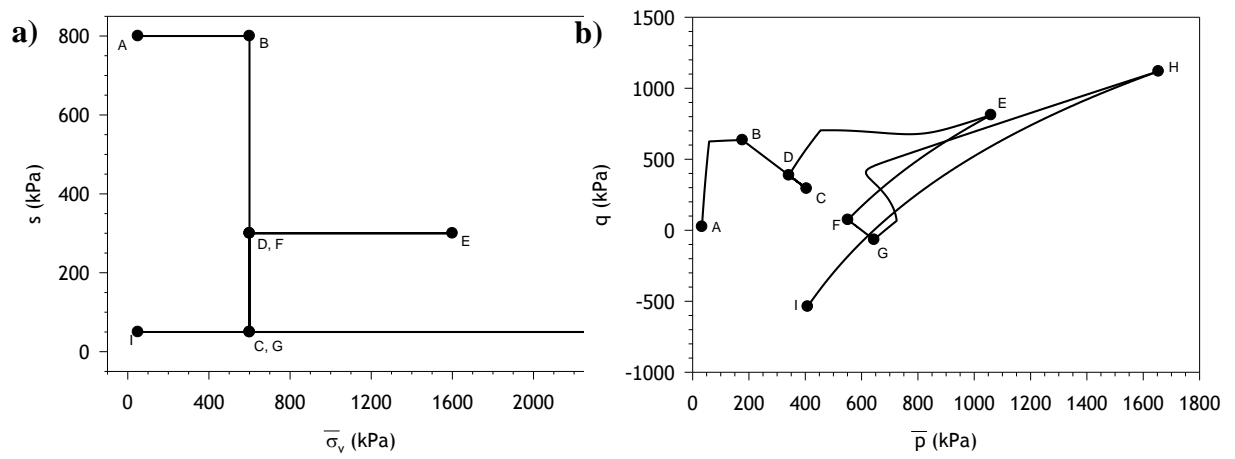


Fig. 14. Oedometer test EDO-1 (a) stress path in $s - \bar{\sigma}_v$ plane; (b) stress path in $q - \bar{p}$ plane predicted by ENPC.

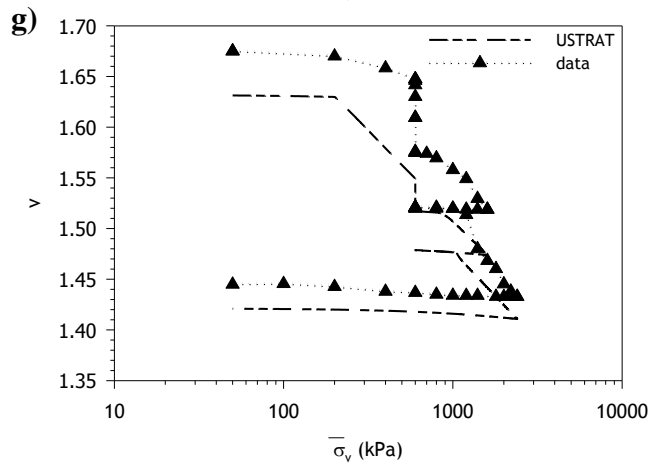
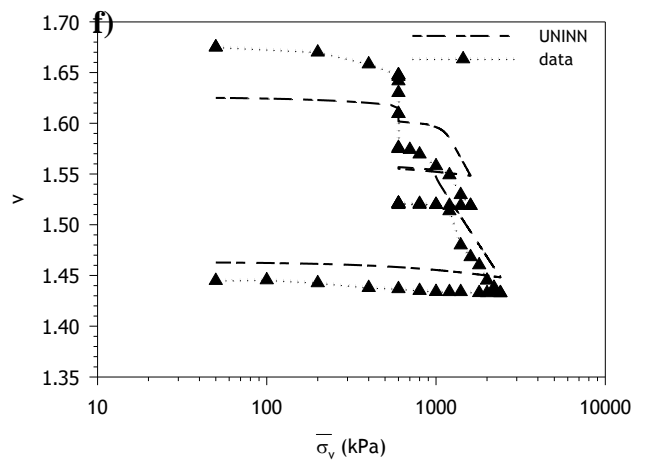
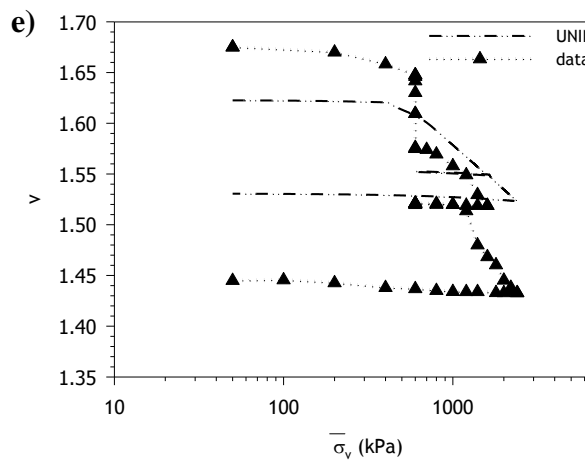
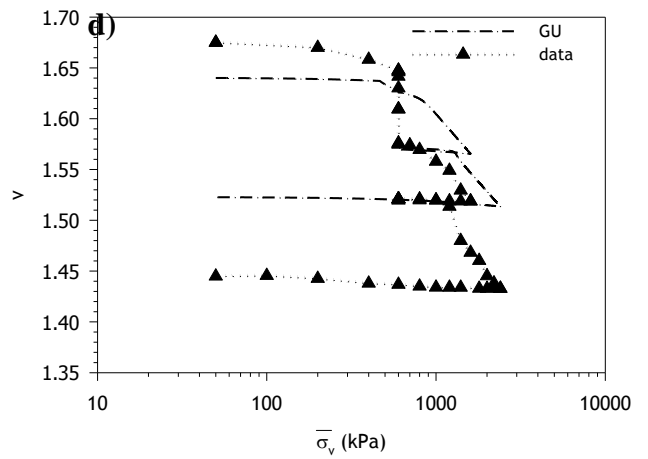
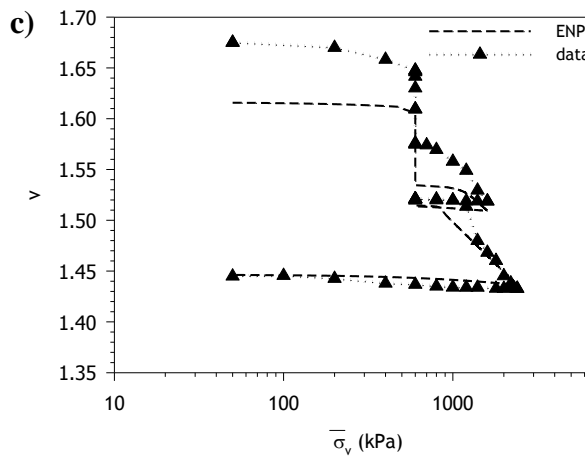
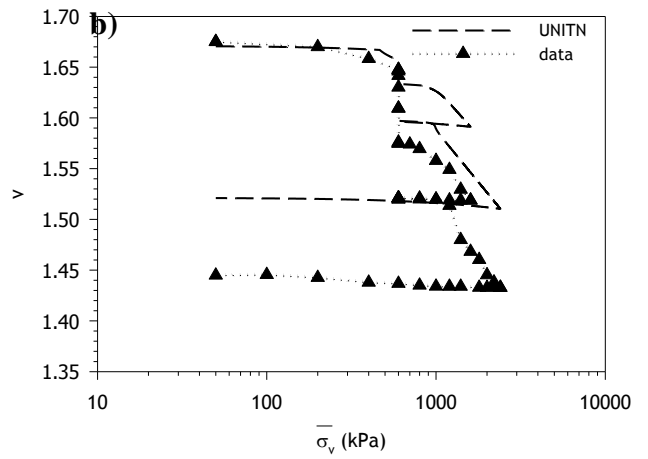
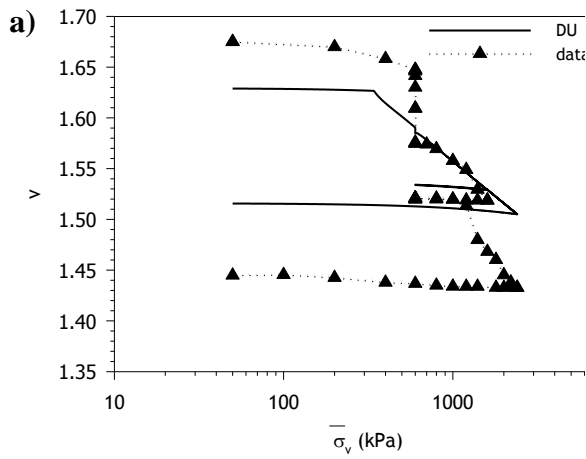


Fig. 15. Simulations and experimental data for suction-controlled oedometer test EDO-1.

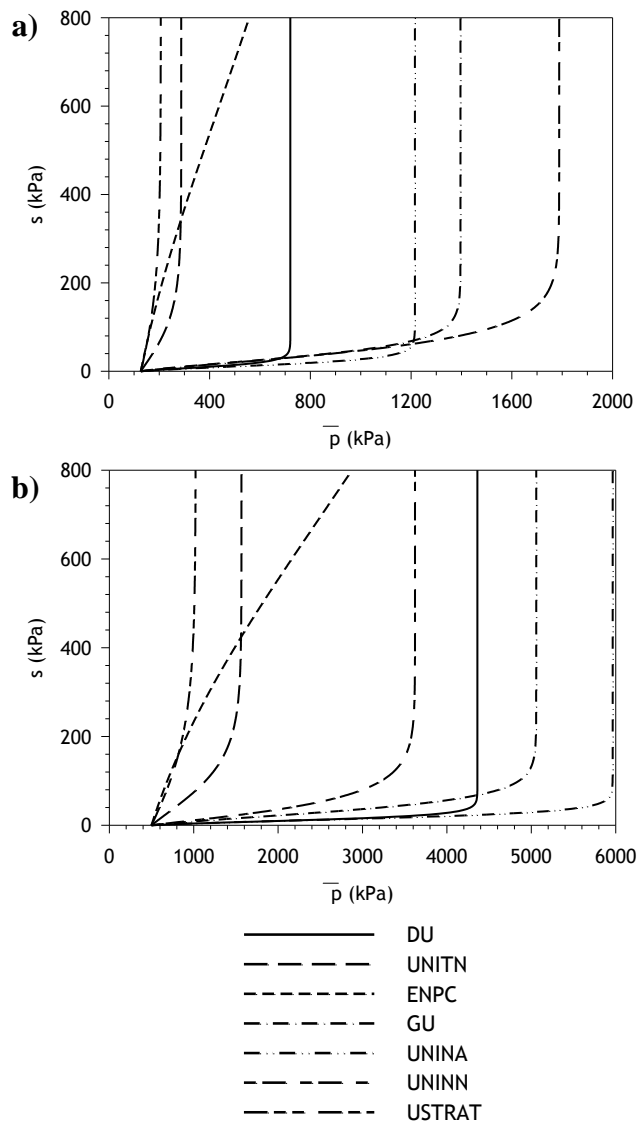


Fig. 16. LC yield curve predicted by different teams for:
(a) $\bar{p}(0) = 120$ kPa; (b) $\bar{p}(0) = 500$ kPa.

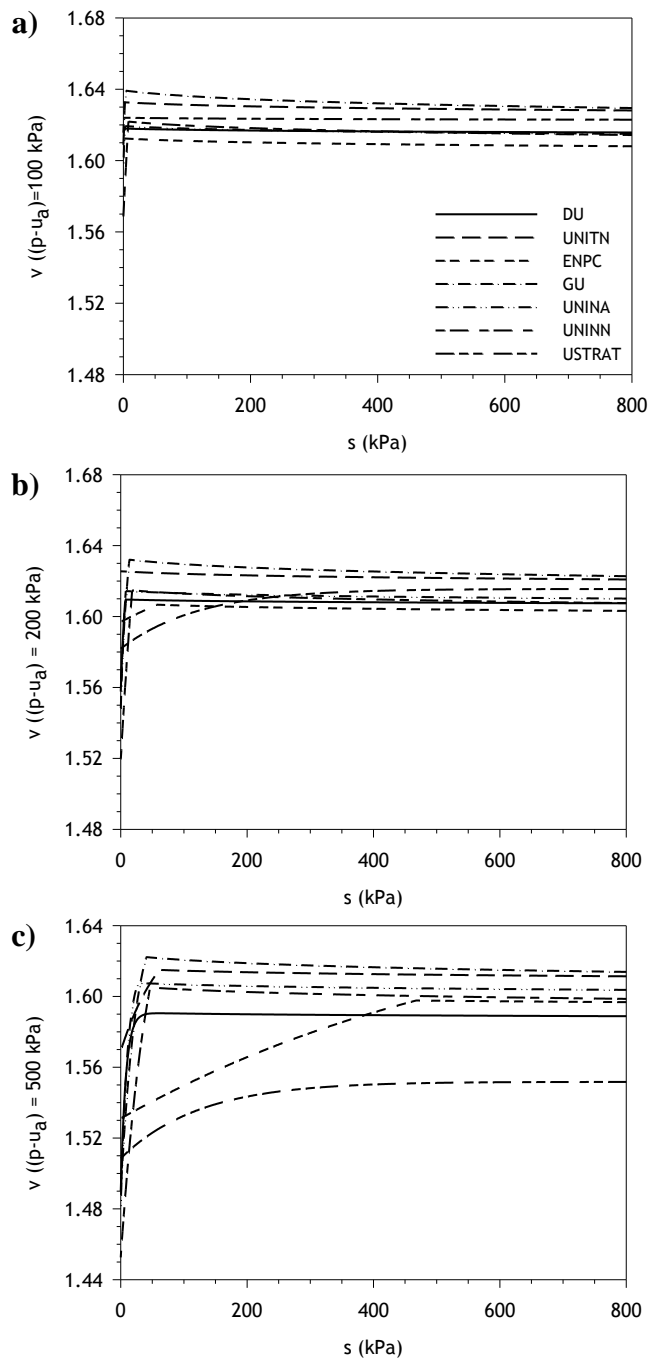


Fig. 17. Predicted variation of specific volume during wetting at a mean net stress of: (a) 100 kPa; (b) 200 kPa; (c) 500 kPa.